



# Introduction to SAR Polarimetry

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ESA–MOST China Dragon 4 Cooperation

**2019 ADVANCED INTERNATIONAL TRAINING COURSE IN LAND REMOTE SENSING**

中欧科技合作“龙计划”第四期 **2019**年陆地遥感高级培训班

18 to 23 November 2019 | Chongqing University, P.R. China



培训时间: 2019年11月18日-23日 主办方: 重庆大学

- **History**
- **Spaceborne Sensors**
- **Basic Concept**
- **PolSAR Processing Chain**

# Discovery of the Phenomena of Polarized Electromagnetic Energy



AD 1000  
Use of the polarized skylight to locate a hidden sun



Crystal of calcite  
Iceland Spar  
Sunstone

1669  
First known  
Quantitative work  
on light observation



Bartholinus

Discovery of the double refraction in calcite



1677  
Wave nature  
of light discovery  
Explanation of the  
double refraction



Huygens

Corpuscular model or  
« longitudinal » waves

1704  
Corpuscular  
Model of light



Newton

1808  
Discovery of the  
polarization of light  
(intrinsic property  
of light and not of  
crystals)



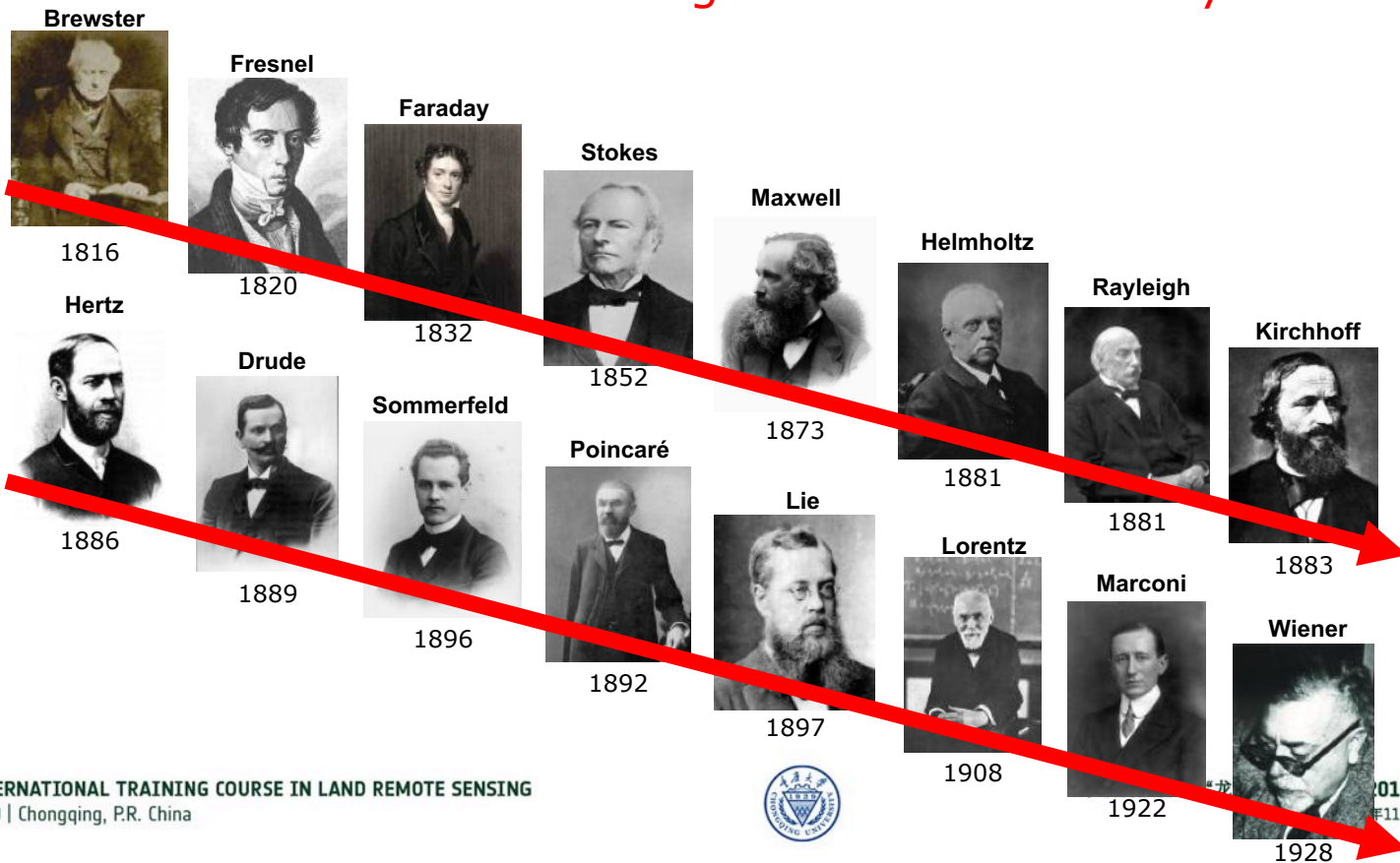
Malus  
X-1795



# Non Exhaustive Chronological List of the Main Pionners who contributed to the discovery



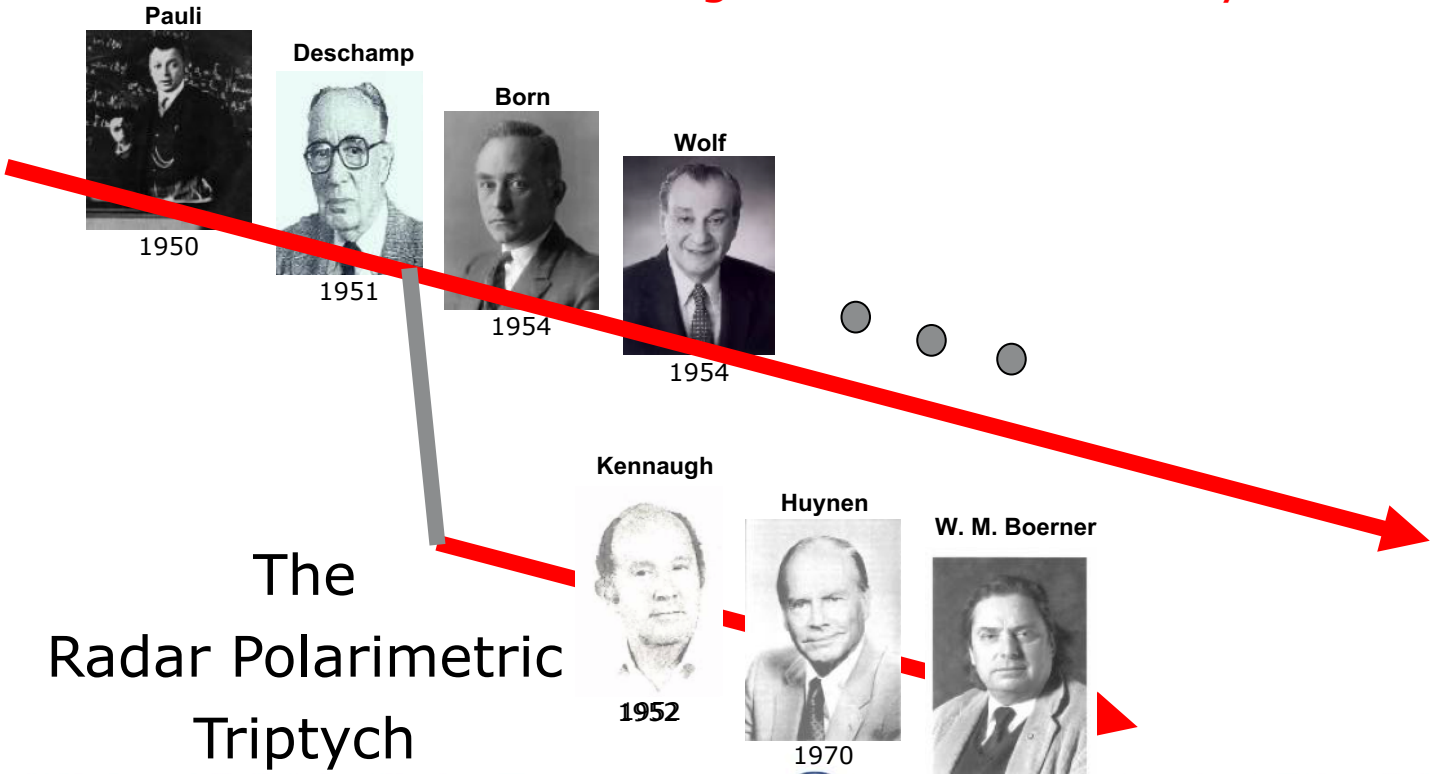
## of Polarization leading to Radar Polarimetry



# Non Exhaustive Chronological List of the Main Pionners who contributed to the discovery



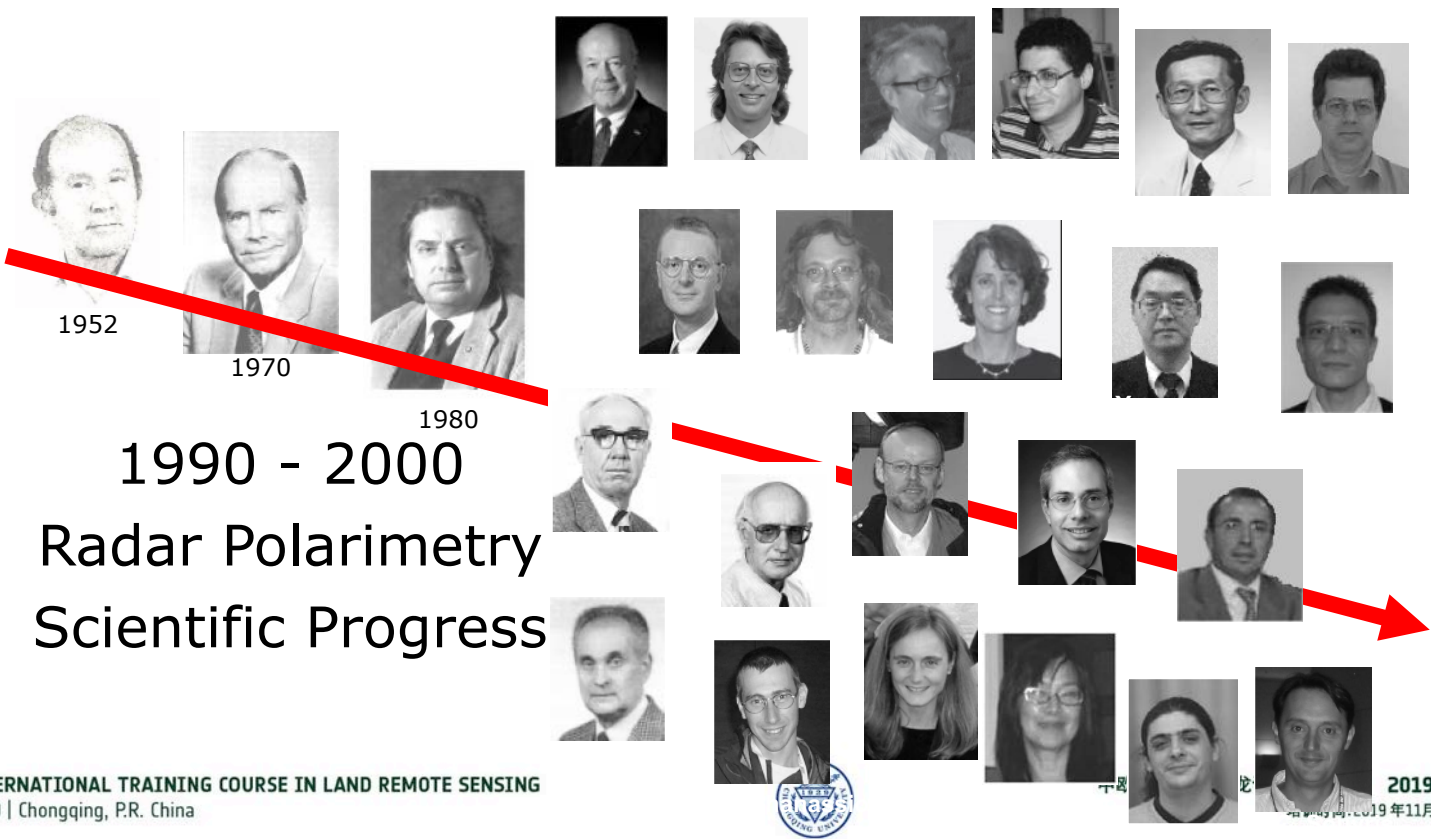
## of Polarization leading to Radar Polarimetry



# Non Exhaustive Chronological List of the Main Pionners who contributed to the discovery



## of Polarization leading to Radar Polarimetry



1952

1970

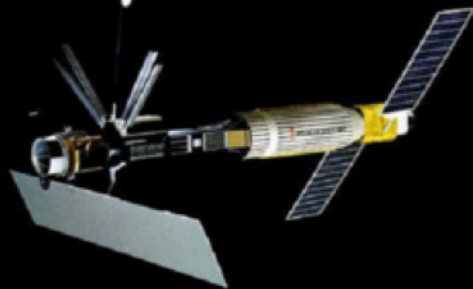
1980

1990 - 2000  
Radar Polarimetry  
Scientific Progress

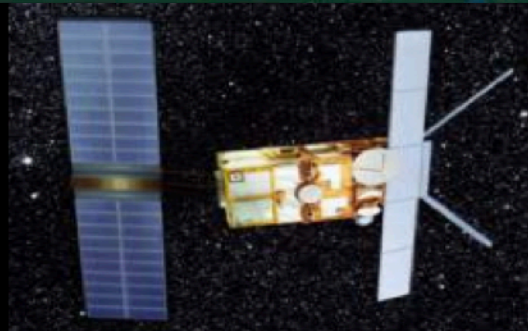


- History
- **Spaceborne Sensors**
- Basic Concept
- **PolSAR Processing Chain**

# Space-borne Sensors



**SEASAT**  
NASA/JPL (USA)  
L-Band, 1978



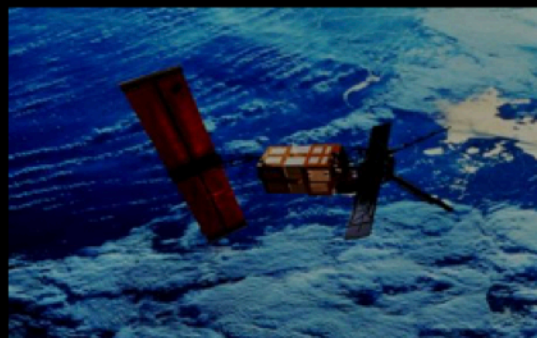
**ERS-1**  
European Space Agency (ESA)  
C-Band, 1991-2000



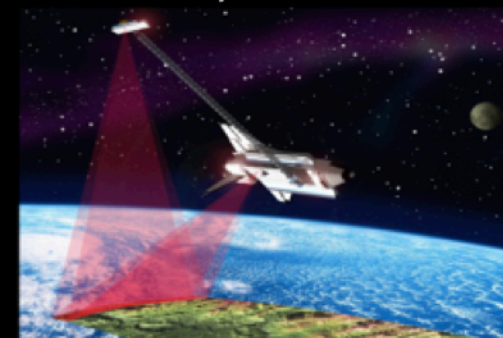
**J-ERS-1**  
Japanese Space Agency (NASDA)  
L-Band, 1992-1998



**RadarSAT-1**  
Canadian Space Agency (CSA)  
C-Band, 1995



**ERS-2**  
European Space Agency (ESA)  
C-Band, 1995



**Shuttle Radar Topography Mission**  
NASA/JPL (C-Band), DLR (X-Band)  
February 2000



## ENVISAT - ASAR

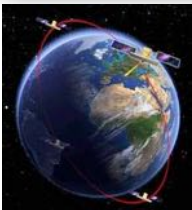
October 2001  
C-Band (Sngl / Dual Inc)



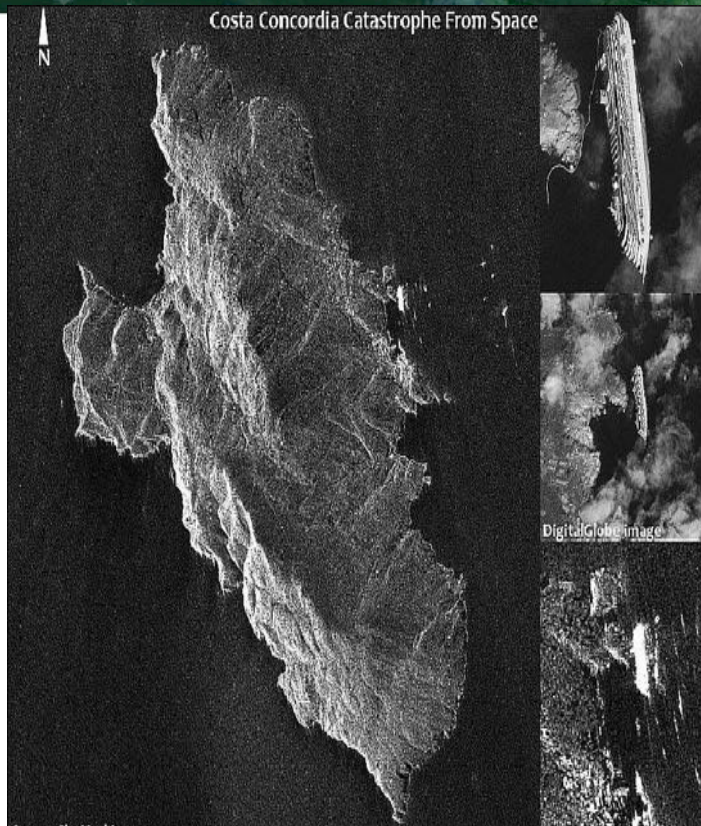
# Space-borne Dual-Pol SAR Sensors



## COSMO - SkyMed



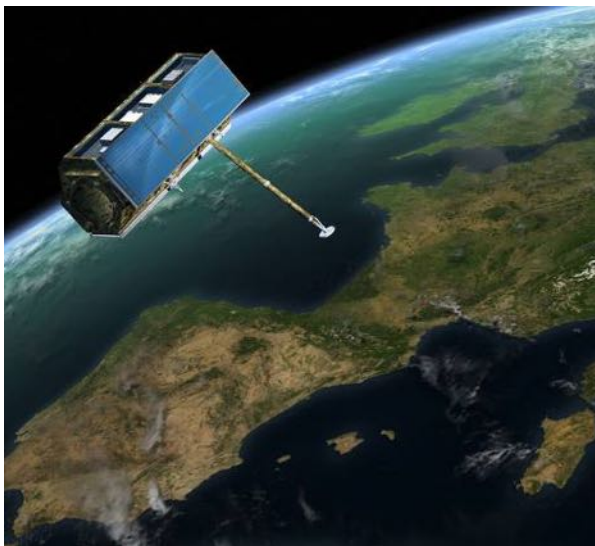
June 2007, Dec. 2007  
Oct. 2008, Nov. 2010  
X-Band (Sngl / Dual)  
Revisit : 1 day



# Space-borne Dual-Pol SAR Sensors



## TerraSAR - X



June 2007

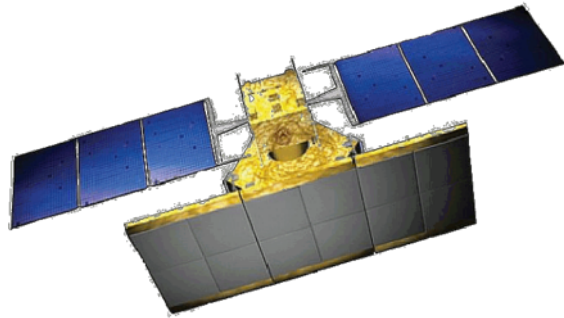
X-Band (Sngl / Twin HH-VV / Quad Exp.)



# Space-borne Dual-Pol SAR Sensors



**RISAT-1A**



**26 April 2012**  
**C-Band (Sngl, Dual, Hybrid)**  
***Operational since 2015***



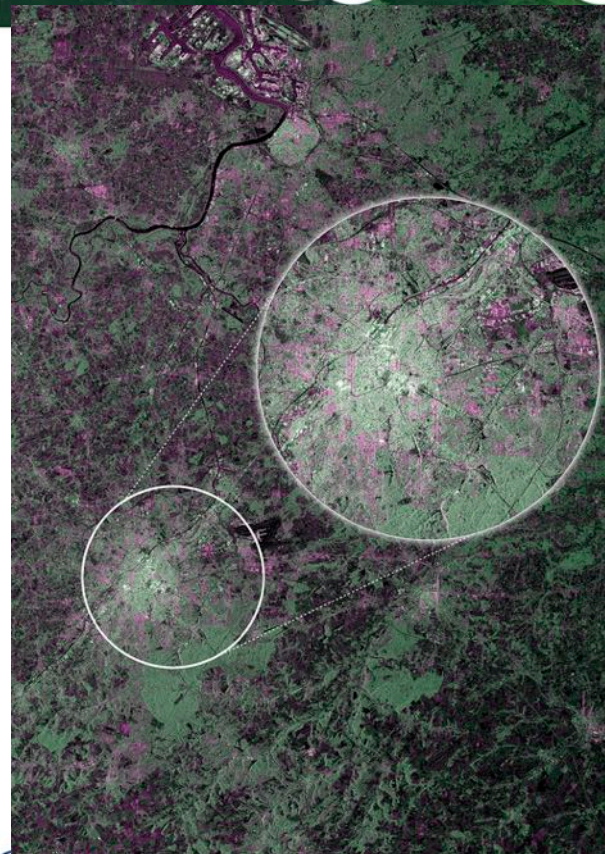
# Space-borne Dual-Pol SAR Sensors



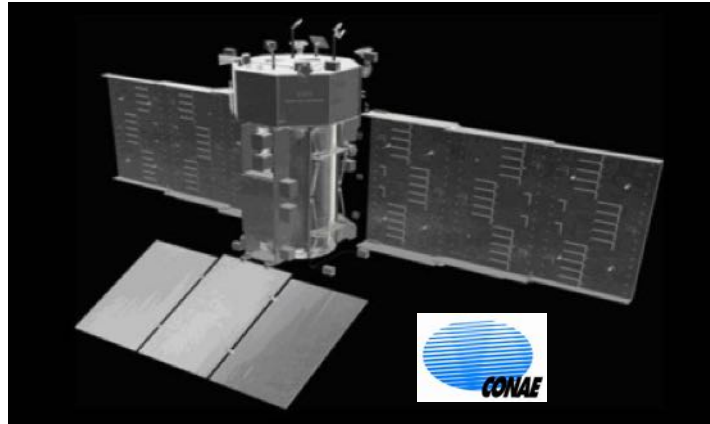
## SENTINEL – 1A/B



**S1A : April 2014    S1B : April 2016**  
**C-Band (Sngl, Dual)**  
**Revisit : 6 days**



## SAOCOM – SAR-L



1A : 2017      1B : 2018

2A : 2019      2B : 2020

L-Band (Sngl, Dual, Twin HH-VV)  
Revisit : 4 days

## RADARSAT Constellation Mission (RCM)



2019 June 12

C-Band (Sngl, Dual, Hybrid)  
Revisit : 4 days

## SIR-C / X-SAR



**April 1994**  
**L- and C-Band (Quad)**  
**X-Band (Sngl)**



**Rwanda, Zaire, Uganda**

## ALOS - PALSAR



January 2006

L-Band (Sngl / Twin / Quad)

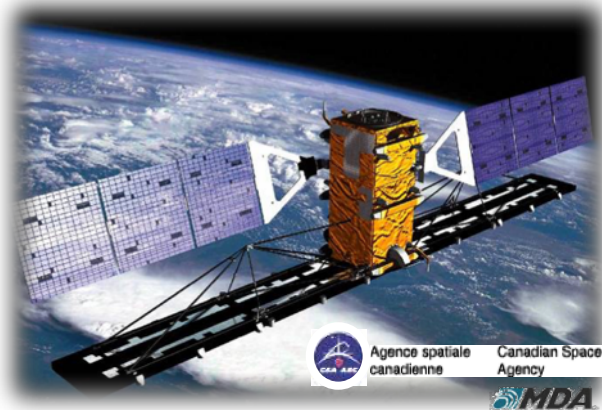


**ALOS : Advanced Land Observing Satellite**  
**PALSAR : Phase Array L-Band SAR**





## RADARSAT - 2



December 2007  
C-Band (Quad)



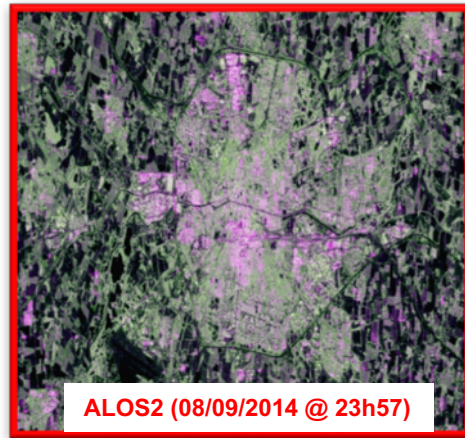
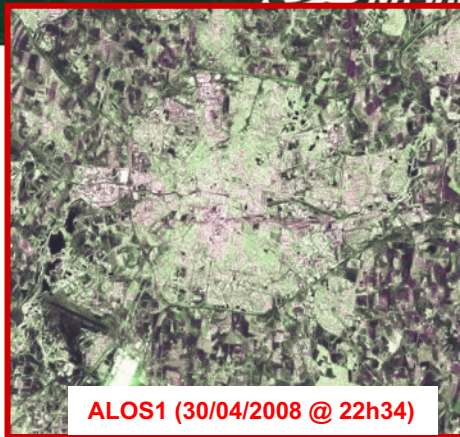
# Space-borne Quad-Pol SAR Sensors



**ALOS - 2**



**May 2014  
L-Band (Quad)**



## GaoFen-3 (GF-3)



August 2016  
C-Band (Quad)



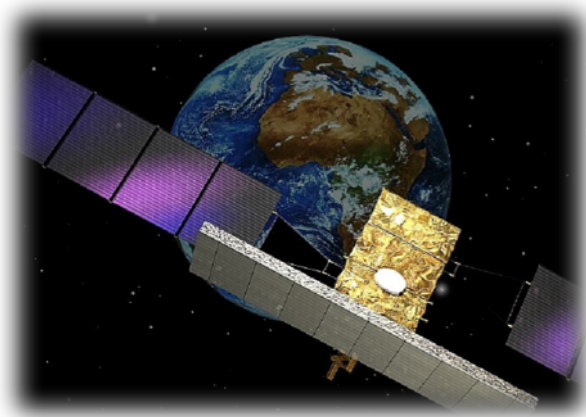
中国空间技术研究院  
China Academy of Space Technology



# Space-borne Quad-Pol SAR Sensors



## COSMO - SkyMed - CSG



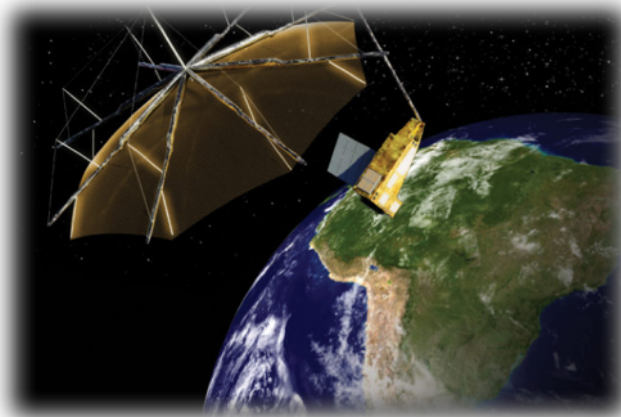
TELESPAZIO  
A Finmeccanica / Thales Company

2A : 2018

2B : 2019

X-Band (Sngl / Dual / Quad Exp.)

## Earth Explorer - BIOMASS

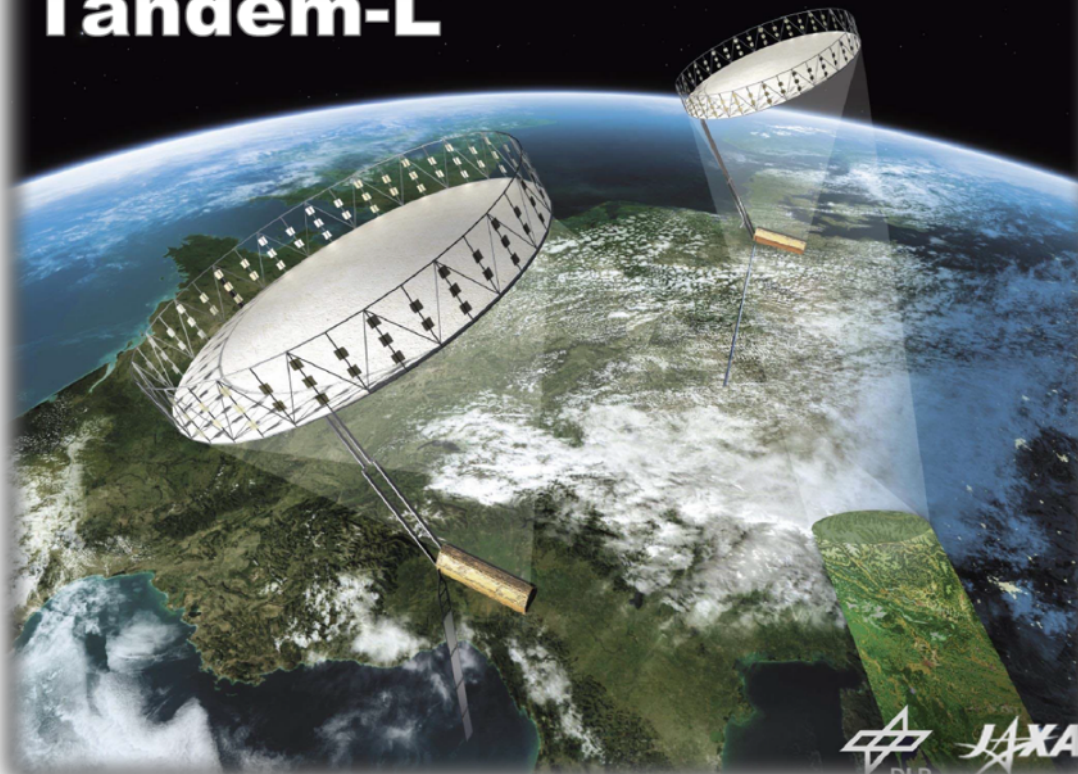


2022

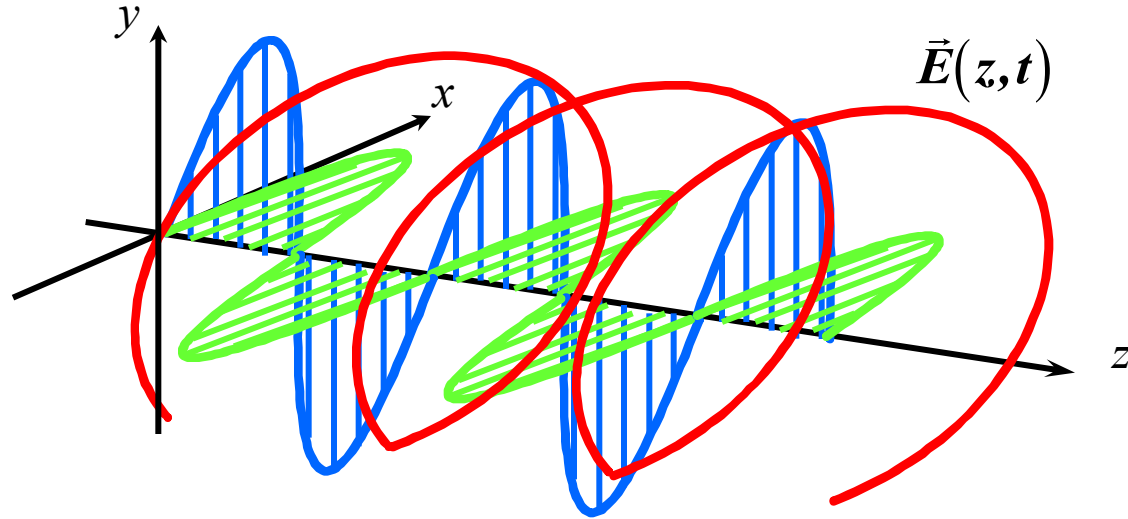
P-Band (Quad)



## Tandem-L

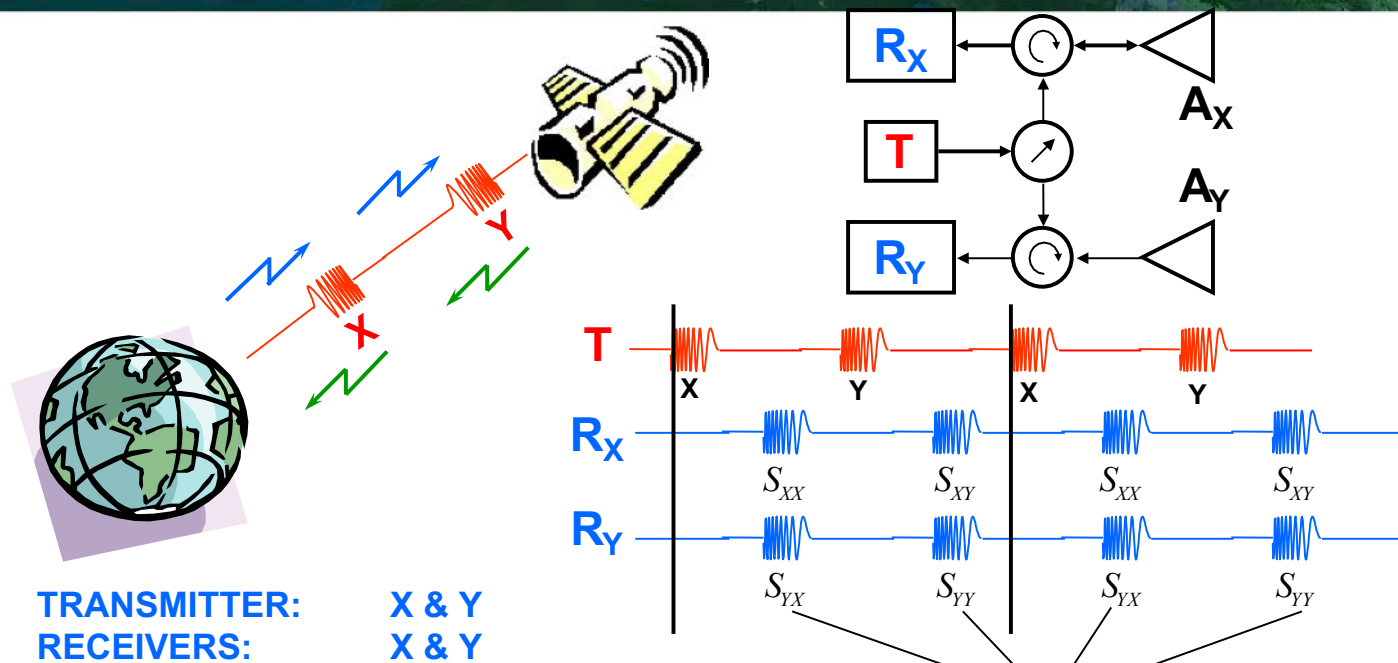


- History
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**Radar Polarimetry (Polar : polarisation Metry: measure)**  
is the, processing and analysing  
the polarization science of acquiring state of an electromagnetic field

# Scattering Polarimetry



SINCLAIR MATRICES

$$\left\{ [S] = \begin{bmatrix} S_{XX} & S_{XY} \\ S_{YX} & S_{YY} \end{bmatrix} \right\}$$





**In monostatic case**

$$S_{hv} = S_{vh}$$

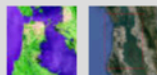
Single Pol	HH	VV	
Dual Pol	HH+HV	VV+HV	HH+VV
Quad Pol	HH+VV+HV		

# GF-3 data download



## GaoFen-3 (GF-3)

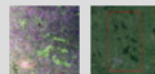
### Full (Quad) Polarimetric Sample Datasets



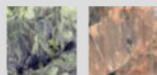
San Francisco Bay (USA) - 2017/09/15



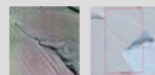
Paris (France) - 2017/09/14



Rennes (France) - 2017/01/03



Skoura (Morocco) - 2017/09/14

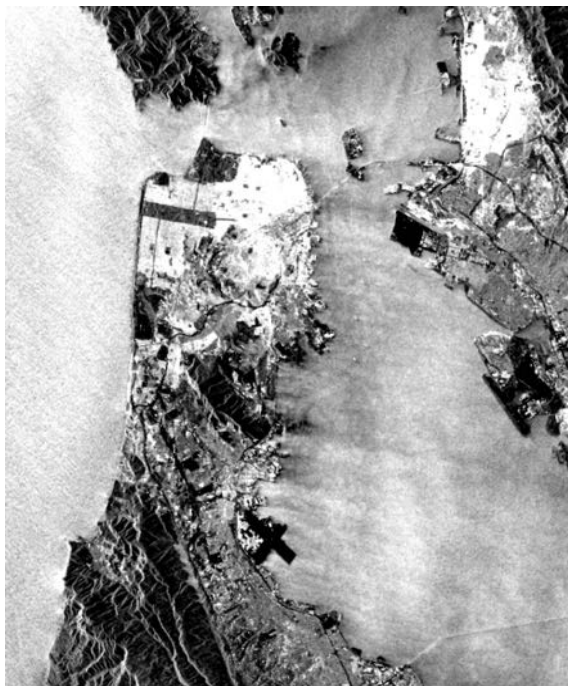


South Pole - 2017/09/16

Visit the [IETR](#) and [IECAS](#) websites

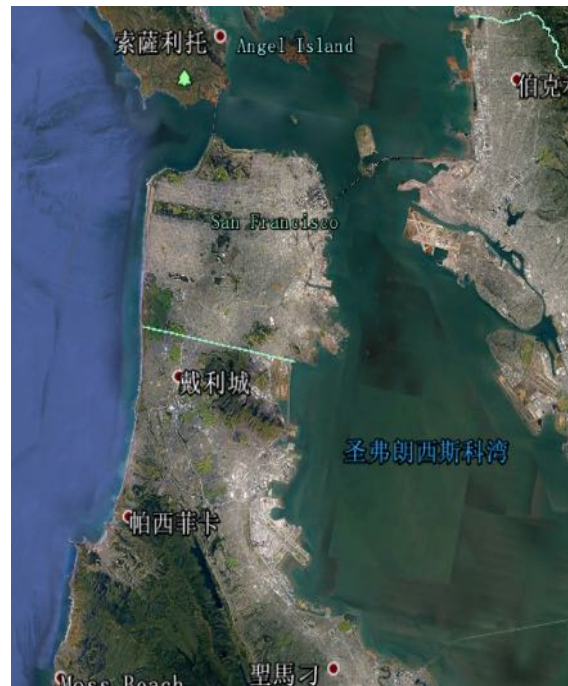
PIWIK Analytics

# GF-3 @ San Francisco



Tx Rx

|HH|<sub>dB</sub>

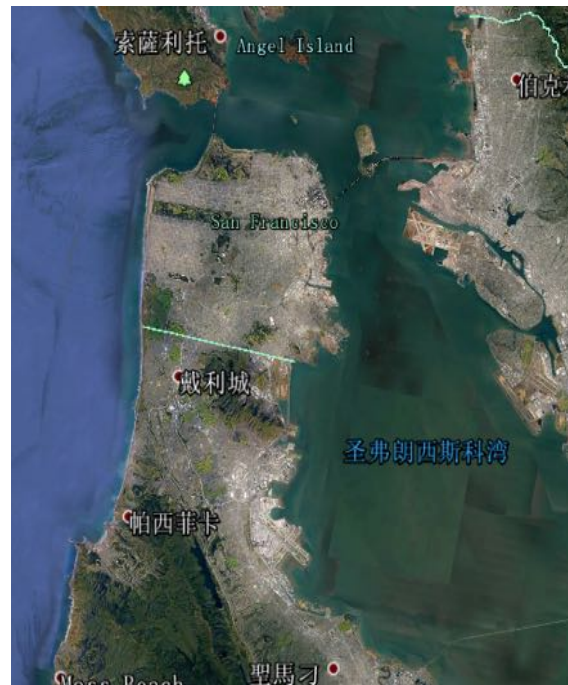


# GF-3 @ San Francisco

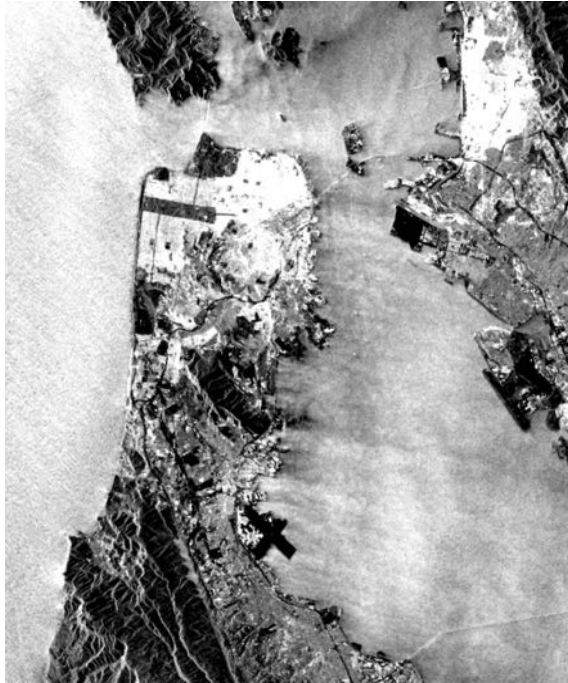


↑ Tx ↑ Rx

$|VV|_{dB}$



# GF-3 @ San Francisco



Tx  
→

Rx  
→

$|HH|_{dB}$



↑ Rx

$|HV|_{dB}$



# GF-3 @ San Francisco



**|HH|<sub>dB</sub>**



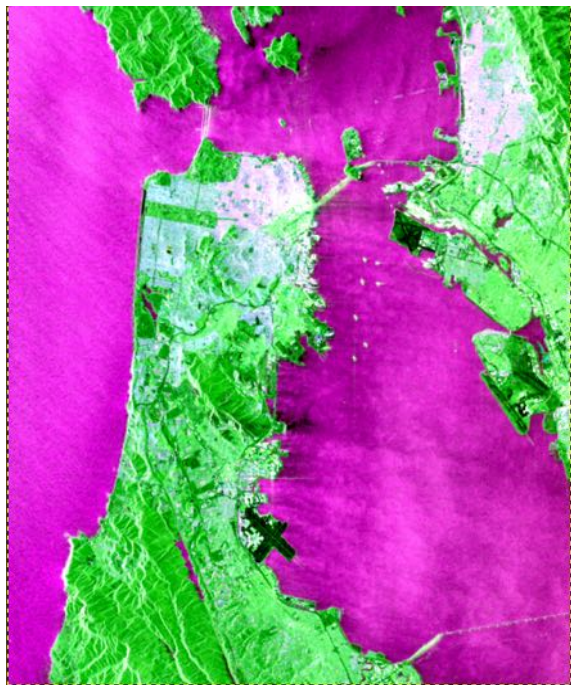
**|HV|<sub>dB</sub>**



**|VV|<sub>dB</sub>**



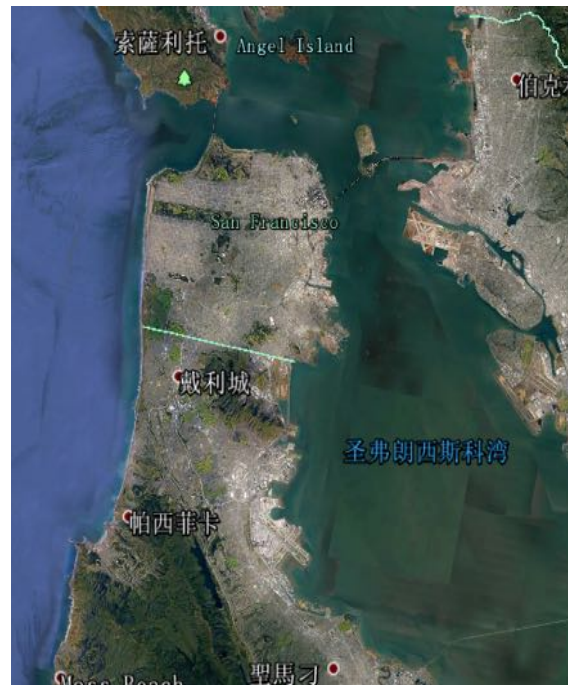
# GF-3 @ San Francisco



$|HH|_{dB}$

$|HV|_{dB}$

$|VV|_{dB}$

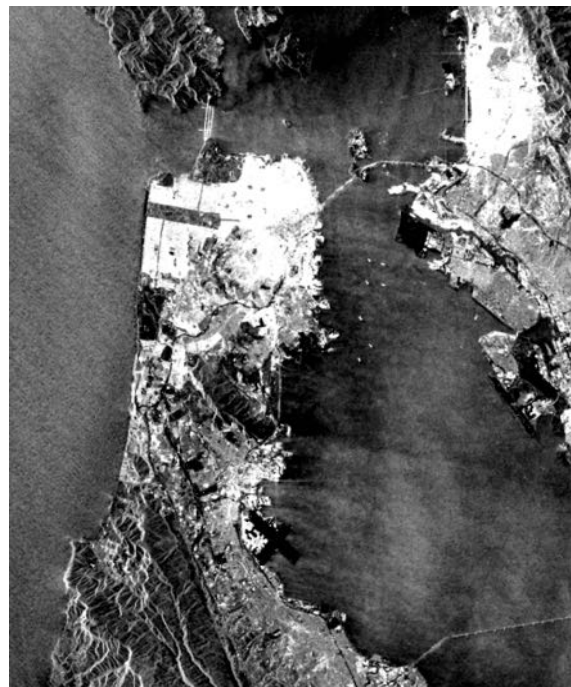


# GF-3 @ San Francisco



**|HH+VV|<sub>dB</sub>**

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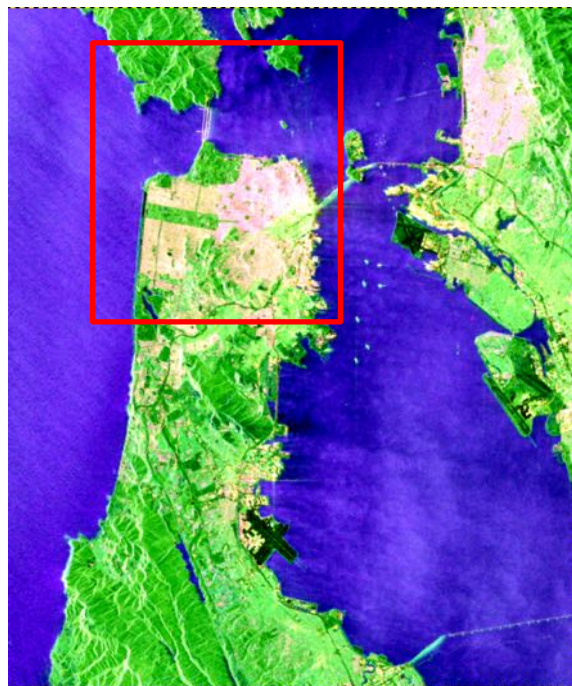
**|HH-VV|<sub>dB</sub>**

中欧科技合作“龙计划”第四期 2019年陆地遥感高级培训班  
培训时间:2019年11月18日-23日 主办方:重庆大学





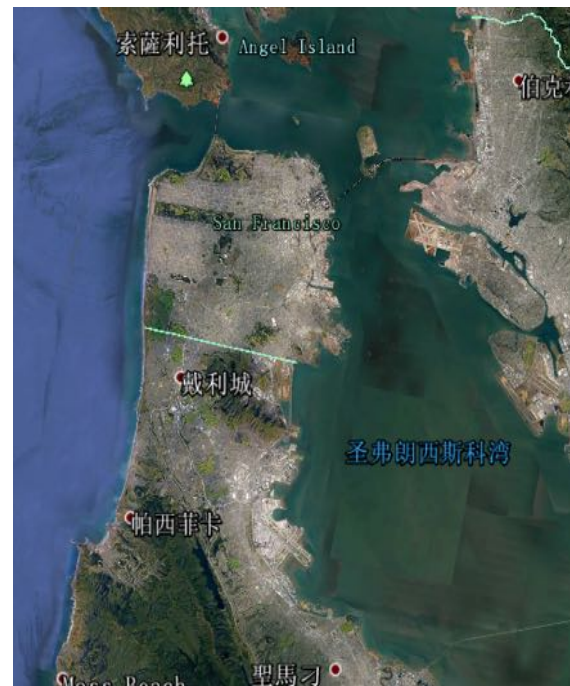
# GF-3 @ San Francisco

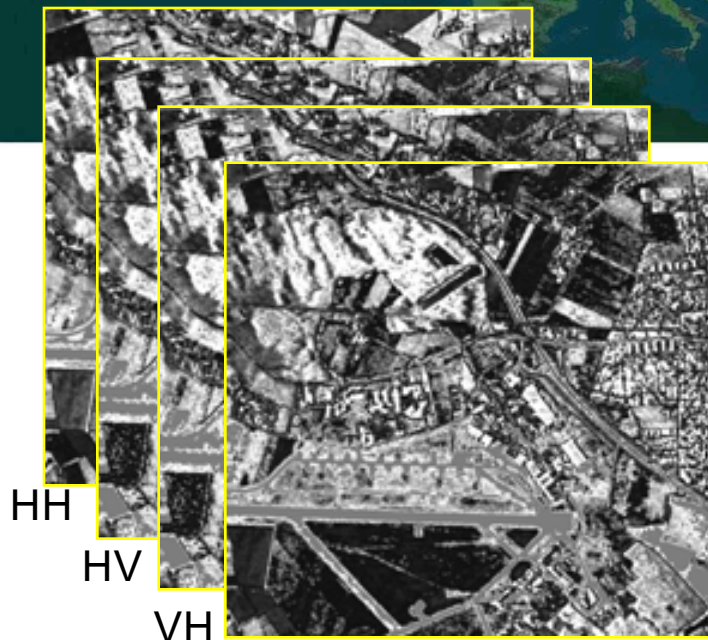


$|HH+VV|_{dB}$

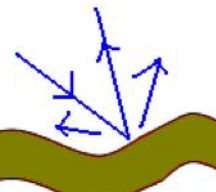
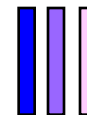
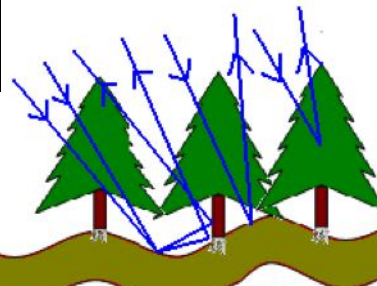
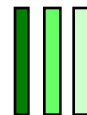
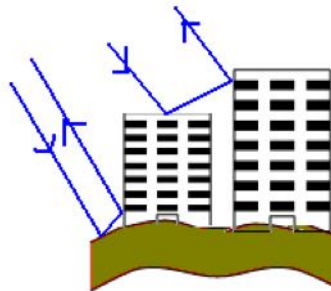
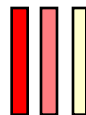
$|HV|_{dB}$

$|HH-VV|_{dB}$



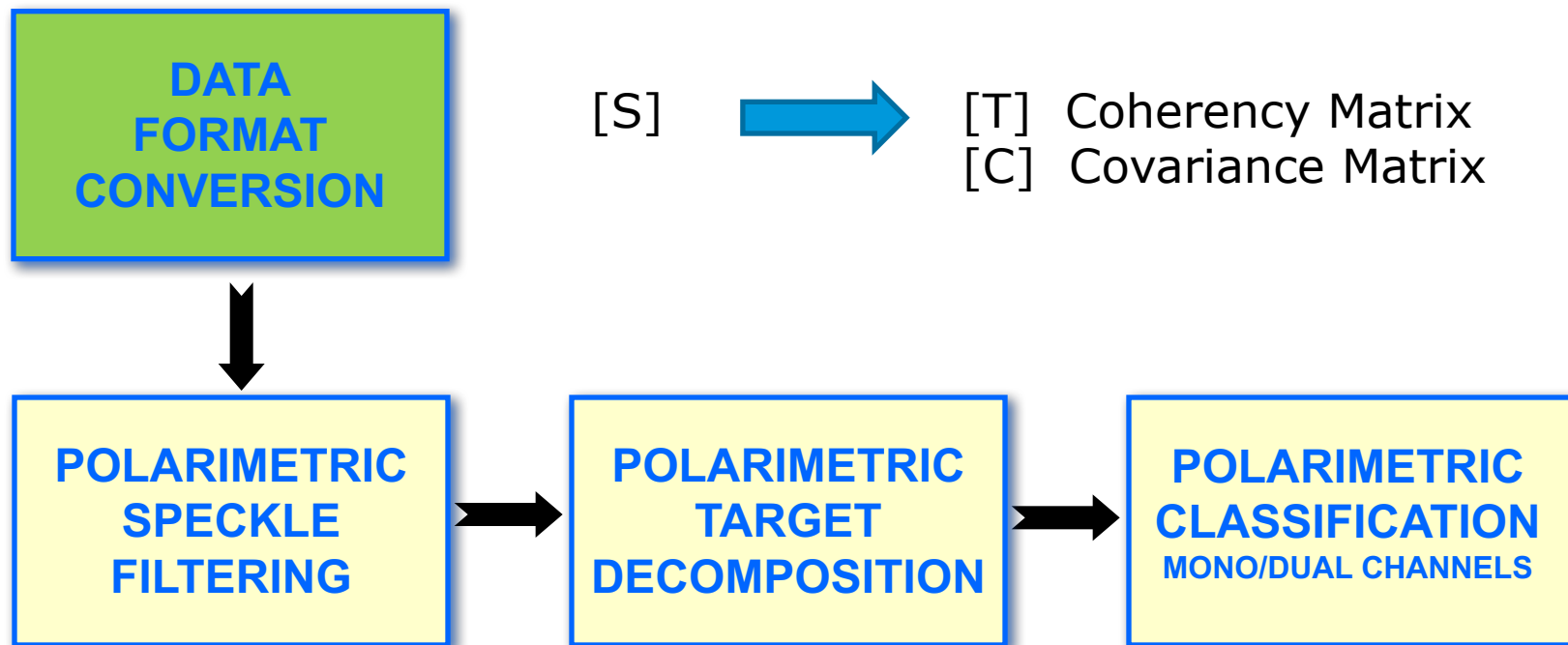


VV



- History
- Spaceborne Sensors
- Basic Concept
- **PolSAR Processing Chain**

# PoSAR Processing Chain



## TARGET VECTOR $\underline{k}$

$$\vec{k}_{3L} = [s_{hh}, \sqrt{2}s_{hv}, s_{vv}]^T$$



$$[C] = \vec{k}_{3L} \vec{k}_{3L}^{*T} = \begin{bmatrix} |s_{hh}|^2 & \sqrt{2}s_{hh}s_{hv}^* & s_{hh}s_{vv}^* \\ \sqrt{2}s_{hv}s_{hh}^* & 2|s_{hv}|^2 & \sqrt{2}s_{hv}s_{vv}^* \\ s_{vv}s_{hh}^* & \sqrt{2}s_{vv}s_{hv}^* & |s_{vv}|^2 \end{bmatrix}$$

## TARGET VECTOR $\underline{k}$

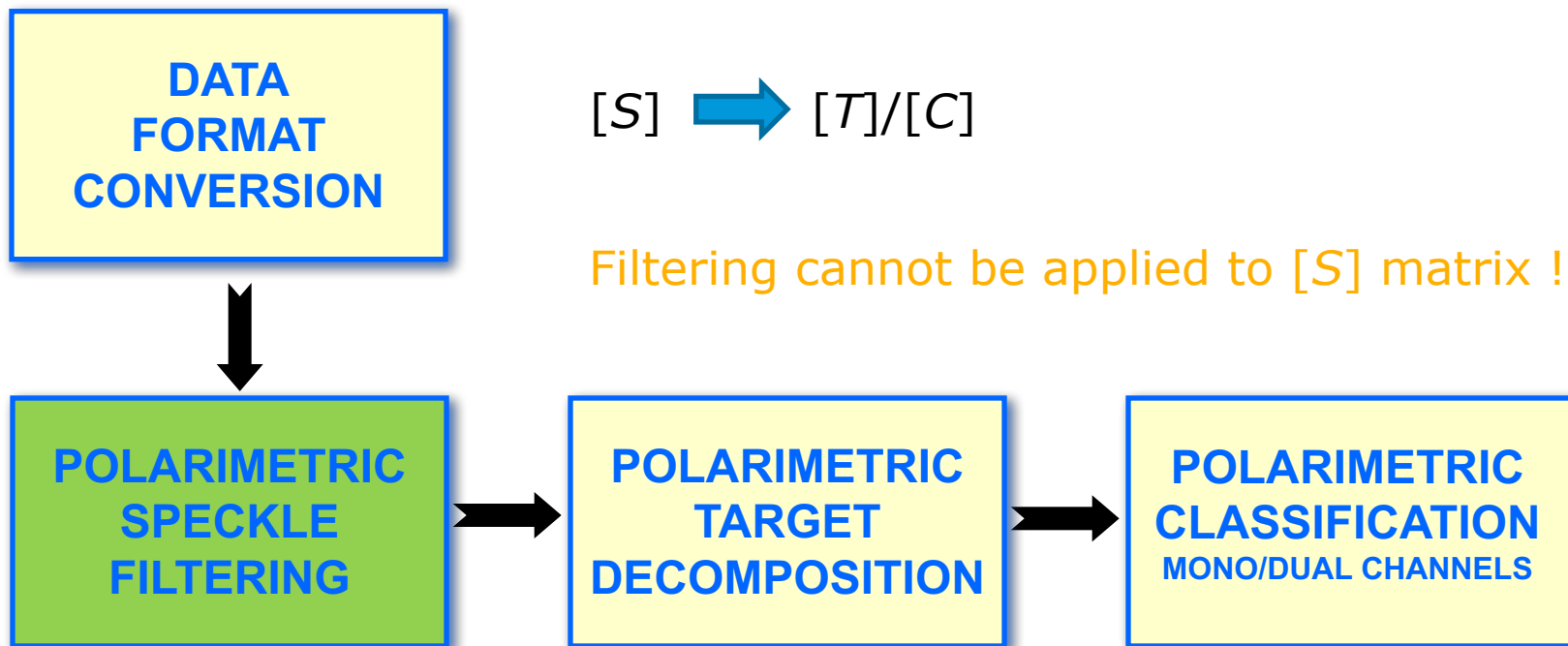
$$\vec{k}_{3P} = [s_{hh} + s_{vv}, s_{hh} - s_{vv}, 2s_{hv}]^T$$



$$[T] = \vec{k}_{3P} \vec{k}_{3P}^{*T} = \frac{1}{2} \begin{bmatrix} |s_{hh} + s_{vv}|^2 & (s_{hh} + s_{vv})(s_{hh} - s_{vv})^* & 2(s_{hh} + s_{vv})s_{hv}^* \\ (s_{hh} - s_{vv})(s_{hh} + s_{vv})^* & |s_{hh} - s_{vv}|^2 & 2(s_{hh} - s_{vv})s_{hv}^* \\ 2s_{hv}(s_{hh} + s_{vv})^* & 2s_{hv}(s_{hh} - s_{vv})^* & 4|s_{hv}|^2 \end{bmatrix}$$

**[T]** is closer related to Physical and Geometrical Properties of the Scattering Process, and thus allows a better and direct physical interpretation

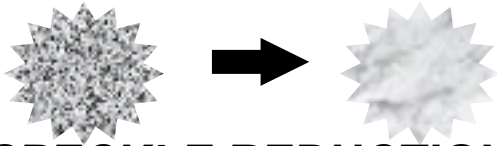
# PoSAR Processing Chain



# Speckle Filtering

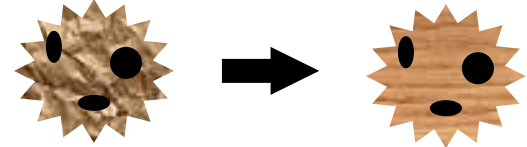


## HOMOGENEOUS AREA



**SPECKLE REDUCTION  
(RADIOMETRIC RESOLUTION)**

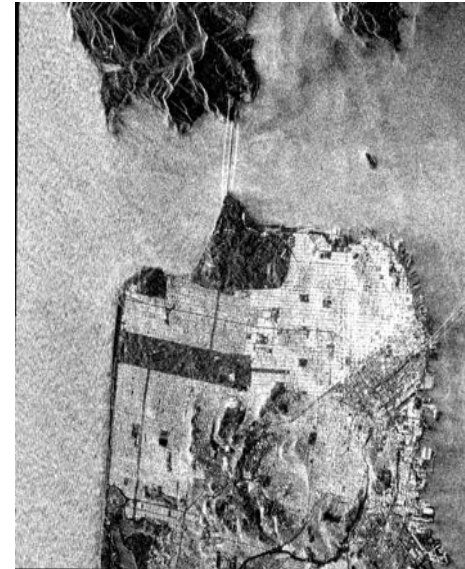
## HETEROGENEOUS AREA



**DETAILS PRESERVATION  
(SPATIAL RESOLUTION)**

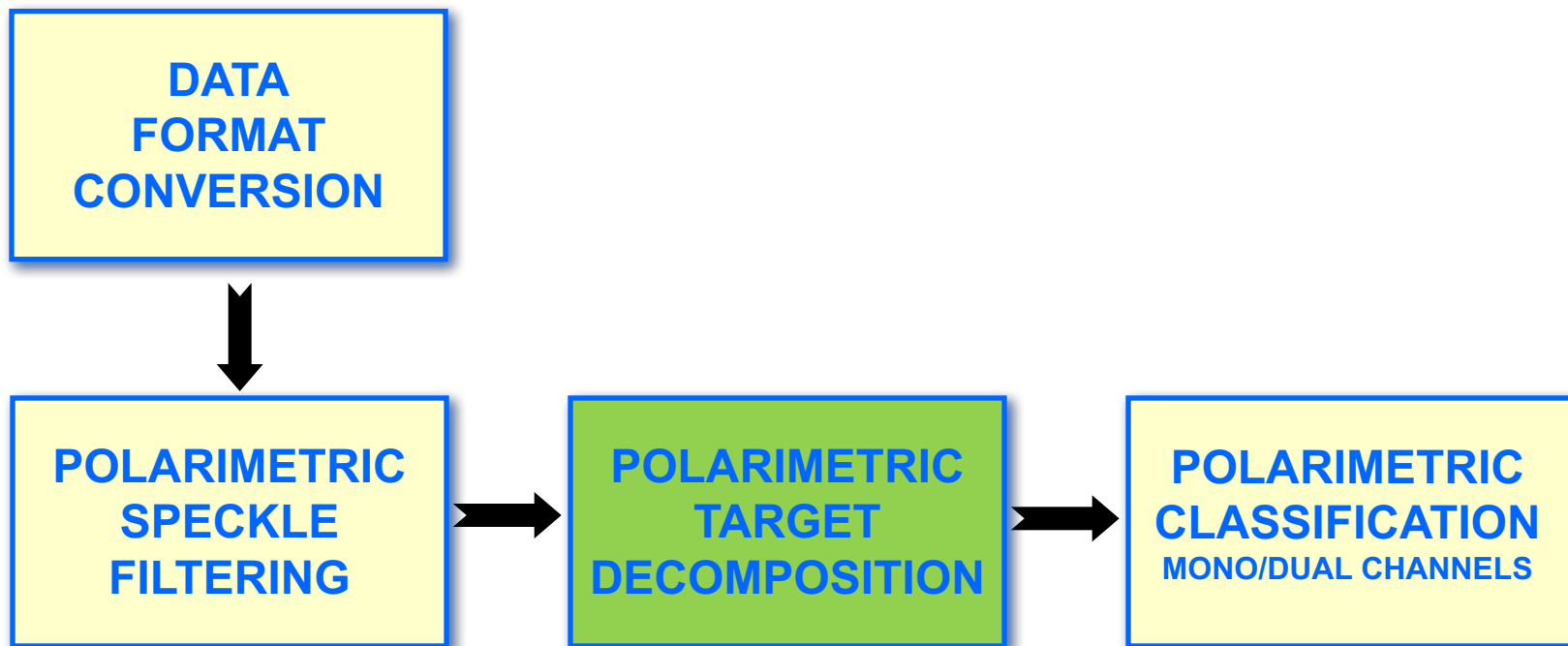


Filtering





# PoSAR Processing Chain



## LOCAL ESTIMATE OF THE COHERENCY MATRIX

$$\langle [T] \rangle = \frac{1}{N} \sum_{i=1}^N \underline{k}_i \cdot \underline{k}_i^{*T} = \frac{1}{N} \sum_{i=1}^N [T_i]$$

## EIGENVECTORS / EIGENVALUES ANALYSIS

$$\langle [T] \rangle = [U_3][\Sigma][U_3]^{-1} = \begin{bmatrix} \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \end{bmatrix} \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \begin{bmatrix} \underline{u}_1 & \underline{u}_2 & \underline{u}_3 \end{bmatrix}^{*T}$$

ORTHOGONAL  
EIGENVECTORS

REAL EIGENVALUES

$$\lambda_1 > \lambda_2 > \lambda_3$$



## PURE TARGET

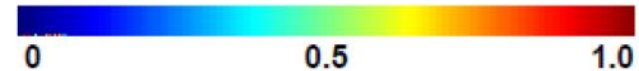
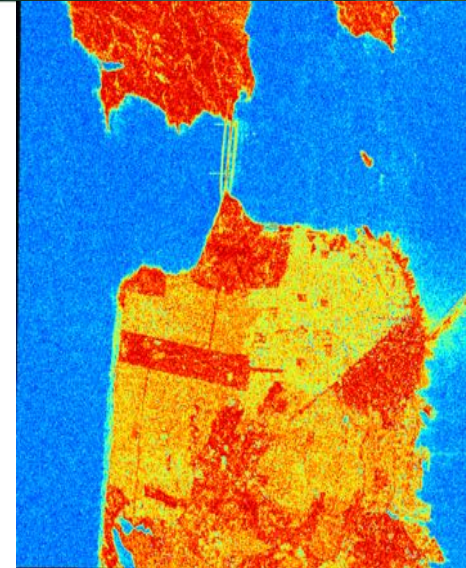
$$\lambda_1 = SPAN \quad \lambda_2 = 0 \quad \lambda_3 = 0$$

$$H = 0$$

## ENTROPY

(DEGREE OF RANDOMNESS  
STATISTICAL DISORDER)

$$H = - \sum_{i=1}^3 P_i \log_3(P_i)$$



## DISTRIBUTED TARGET

$$\lambda_1 = \lambda_2 = \lambda_3 = SPAN / 3$$

$$H = 1$$



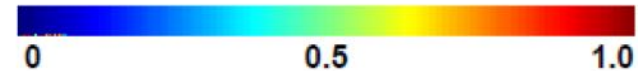
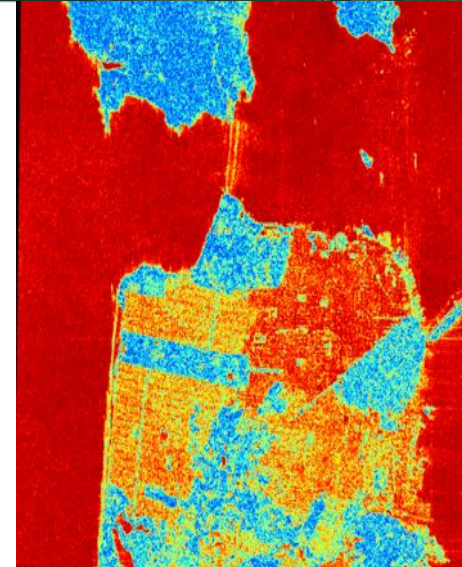
## ANISOTROPY (EIGENVALUES SPECTRUM)

$$A = \frac{\lambda_2 - \lambda_3}{\lambda_2 + \lambda_3}$$

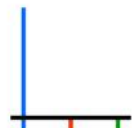


COMPLEMENTARY TO ENTROPY  
DISCRIMINATION WHEN  $H > 0.7$

ROLL INVARIANT



**(1-H)(1-A)**

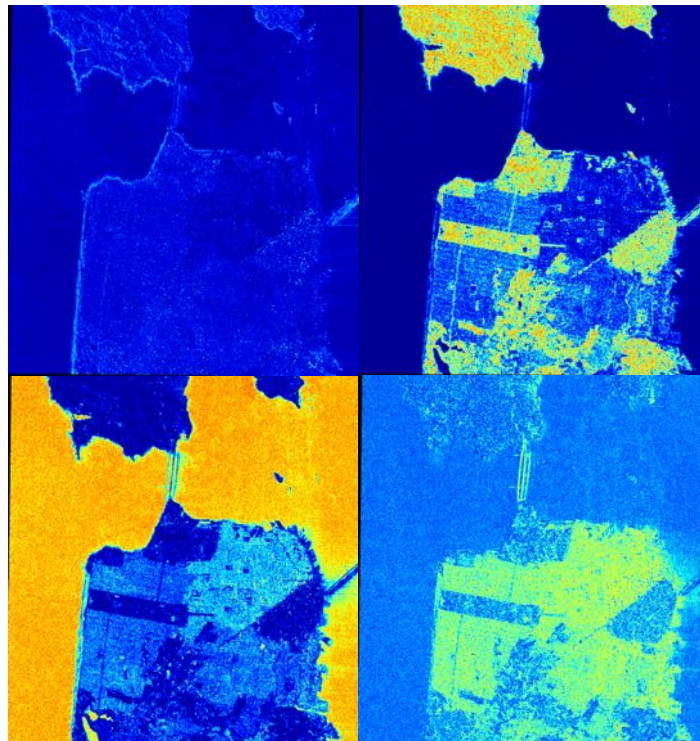


1 MECHANISM

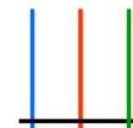
**A(1-H)**



2 MECHANISMS

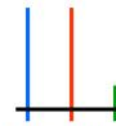


**H(1-A)**



3 MECHANISMS

**HA**



2 MECHANISMS

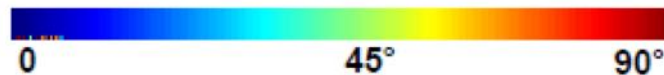
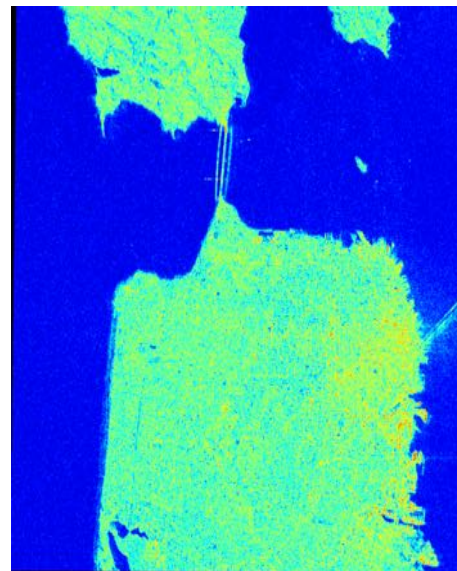
## EIGENVECTOR MATRIX PARAMETER

$$[U_3] = \begin{bmatrix} \cos \alpha_1 e^{j\phi_1} & \cos \alpha_2 e^{j\phi_2} & \cos \alpha_3 e^{j\phi_3} \\ \sin \alpha_1 \cos \beta_1 e^{j\phi_1} e^{j\delta_1} & \sin \alpha_2 \cos \beta_2 e^{j\phi_2} e^{j\delta_2} & \sin \alpha_3 \cos \beta_3 e^{j\phi_3} e^{j\delta_3} \\ \sin \alpha_1 \sin \beta_1 e^{j\phi_1} e^{j\gamma_1} & \sin \alpha_2 \sin \beta_2 e^{j\phi_2} e^{j\gamma_2} & \sin \alpha_3 \sin \beta_3 e^{j\phi_3} e^{j\gamma_3} \end{bmatrix}$$

TARGET 1
TARGET 2
TARGET 3

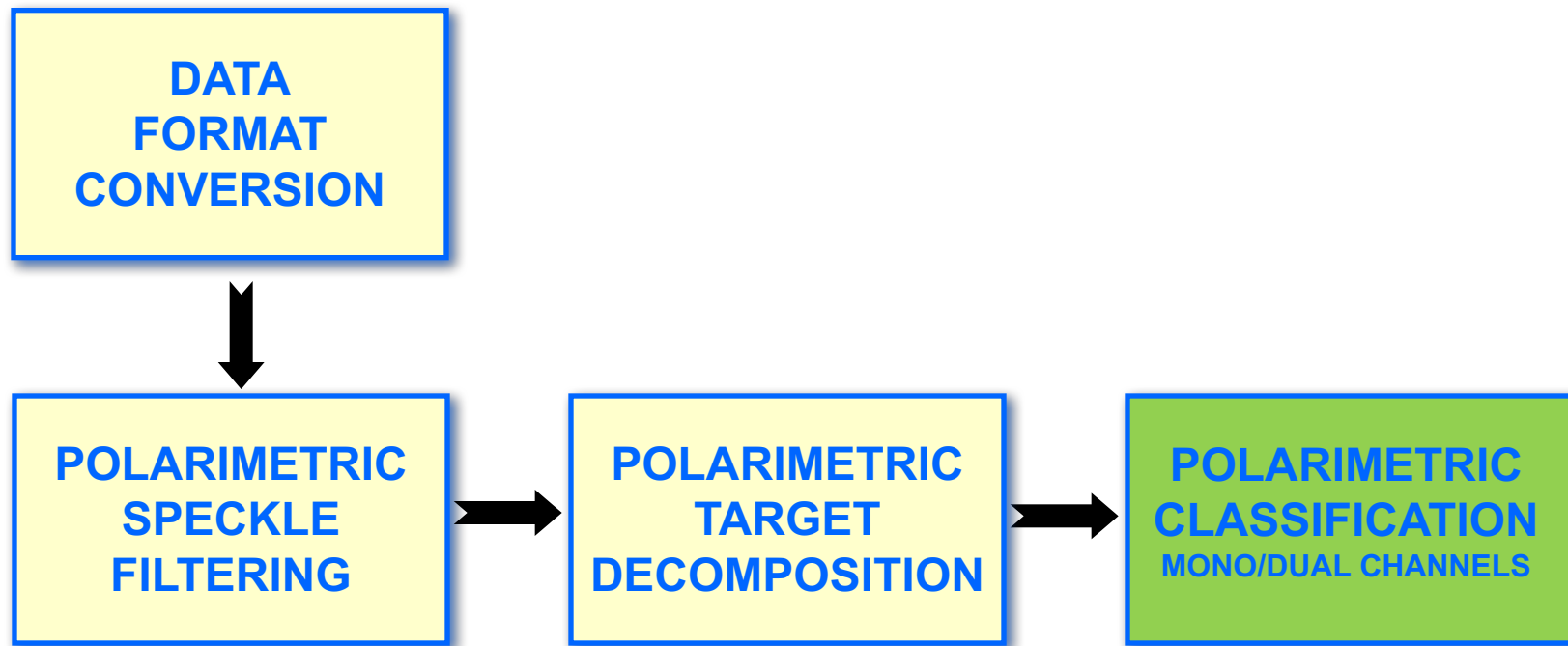


$$\alpha = p_1 \alpha_1 + p_2 \alpha_2 + p_3 \alpha_3$$



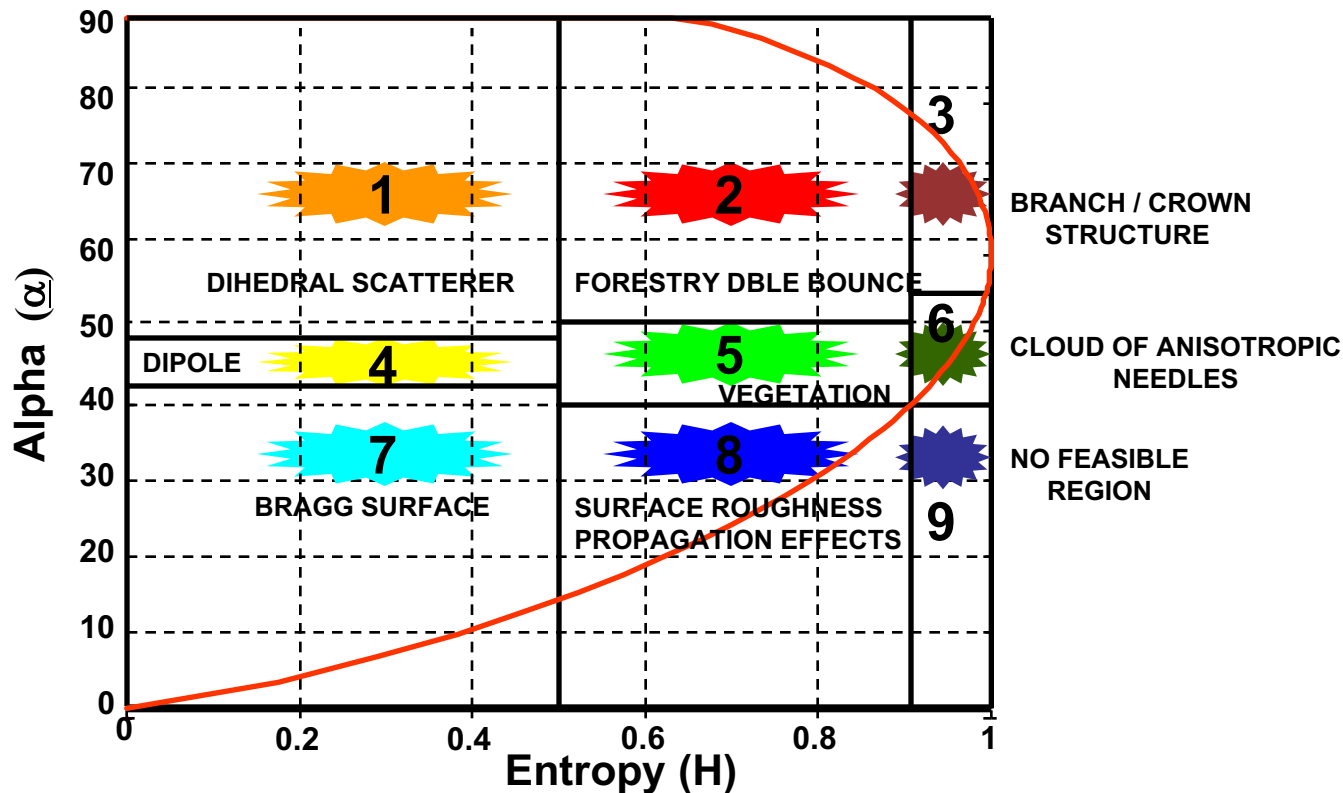
$\alpha$  PARAMETER

# PoSAR Processing Chain

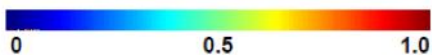
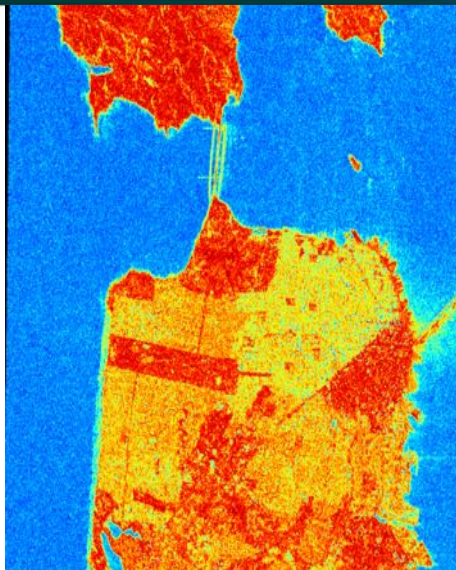




# H / $\alpha$ CLASSIFICATION



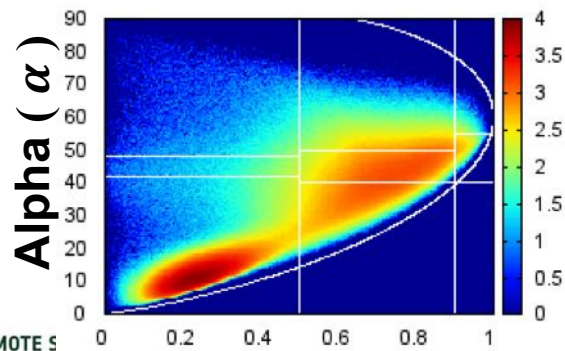
# H / $\alpha$ CLASSIFICATION



H

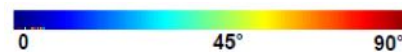
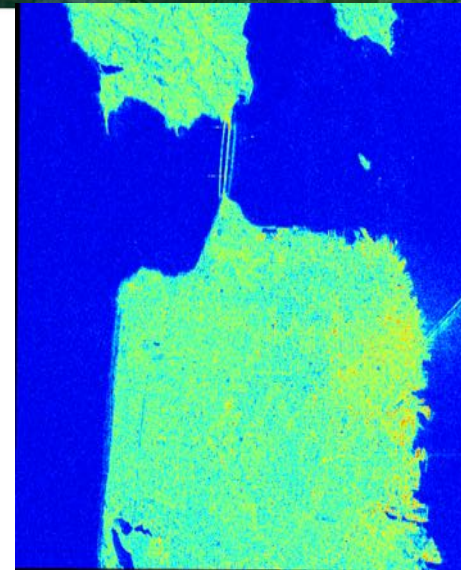


## POLSAR DATA DISTRIBUTION IN THE H / $\alpha$ PLANE



ND REMOTE S

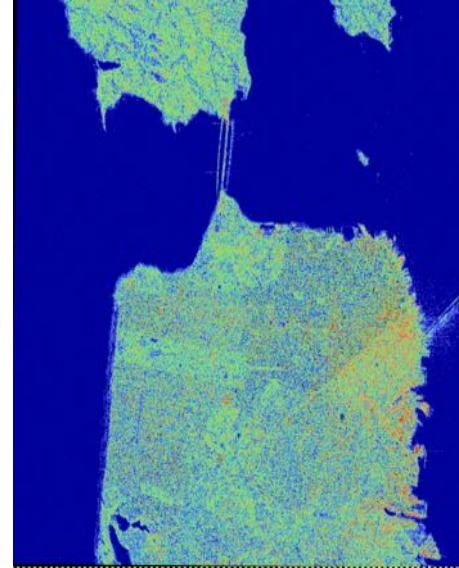
Entropy (H)



$\alpha$



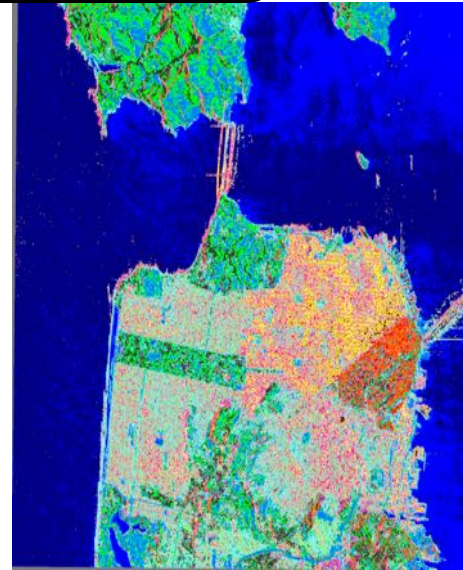
中欧



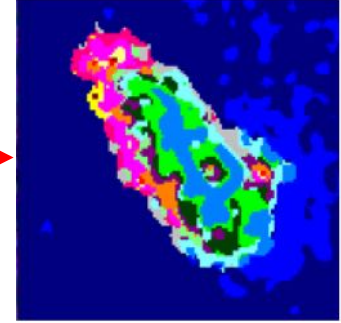
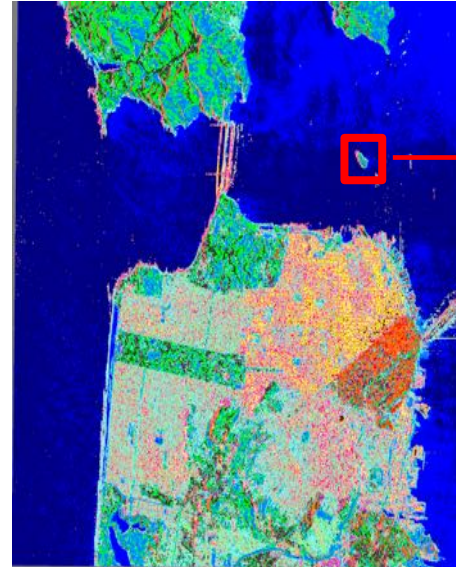
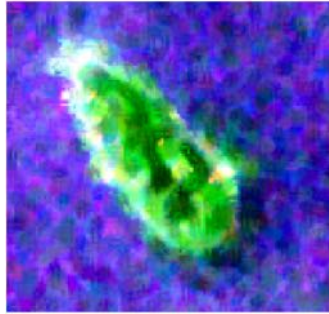
H -  $\alpha$  classification

**WISHART PDF**

$$P(\langle [T] \rangle / [T_m]) = \frac{L^L p |\langle [T] \rangle|^{L-p} e^{-L \text{Tr}([T_m]^{-1} \langle [T] \rangle)}}{\pi^{\frac{p(p-1)}{2}} \Gamma(L) \dots \Gamma(L-p+1) [T_m]^L}$$



# WISHART H / A / $\alpha$ CLASSIFICATION



# POLSAR BOOKS



## Polarimetric Radar Imaging: From basics to applications

*Jong-Sen LEE – Eric POTTIER*

CRC Press; 1st ed., February 2009, pp 422

TRANSLATION By Wen HONG's group

## Polarisation: Applications in Remote Sensing

*Shane R. CLOUDE*

Oxford University Press, October 2009, pp 352

COURSE IN LAND REMOTE SENSING



中欧科技合作





# Introduction to SAR Polarimetry

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ESA–MOST China Dragon 4 Cooperation

**2019 ADVANCED INTERNATIONAL TRAINING COURSE IN LAND REMOTE SENSING**

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