

1 Sampling for validation of ecotope maps
2 of floodplains in the Netherlands

3 M. Knotters¹ D.J. Brus¹

4 ¹Soil Science Centre, Wageningen University and Research Centre, P.O. Box 47, 6700 AA Wa-
5 geningen, The Netherlands, email: martin.knotters@wur.nl, dick.brus@wur.nl

Abstract

Ecotope maps of five districts of main water courses in the Netherlands are validated on the basis of independent samples of field observations. Total map purity, and user's and producer's accuracy for each map unit were estimated. In four districts the validation samples were selected purposively in the past. For the fifth district a stratified two-stage probability sample was designed, such that the spatial pattern resembles that of the purposive samples. For the maps of the purposively sampled districts ratio-estimators of quality measures are calculated following a model-based approach, using a model for the spatial variation of classification errors. For the map of the randomly sampled district ratio-estimators of quality measures are obtained following a design-based approach, using the selection probabilities of the sampling points. Both user's and producer's accuracies show large variation among the map units, depending on the contribution of several sources of error in the mapping process and on observation errors during the fieldwork for validation. The total map purities vary from 56 to 76 %. We demonstrate that stratified two-stage sampling is an alternative to purposive sampling, answering to the same practical and budgetary constraints. Stratified two-stage sampling combined with a design-based estimation method results in model-free estimates of map purity, user's and producer's accuracies. This is an important advantage in validation, because the results do not depend on the quality of model assumptions. This means that the validity of the estimated map purities, user's and producer's accuracies is beyond discussion if a design-based approach is followed.

1 Introduction

An ecotope is defined as a spatially bounded ecological unit, which composition and development are determined by abiotic, biotic and anthropogenic aspects (Wolfert, 1996; Stumpel and Kalkhoven, 1978; Girel et al., 1997). Ecotopes are more or less homogeneous units at landscape scale, which are discernible from similarities and contrasts in geomorphology and hydrology, vegetation structure and land use. Ecotope maps are used as basic information for policy- and management purposes, regarding water quantity (safety, EU Flood Directive), water quality (EU Water Framework Directive), ecological system knowledge (Flora- and Fauna Law, Nature Protection Law, EU Birds and Habitats Directive) and restoration- and development projects of the Dutch water systems. Ecotopes are monitored by surveys that are repeated each six years.

Ecotope maps have been made for five districts of the main watercourses in the Netherlands (Figure 1), in 2004 (Maas, IJsselmeer), 2005 (Rijntakken, Volkerak-Zoommeer) and 2006 (Rijn-Maasmonding). An ecotope map is a result of combining different kind of information layers by an overlay procedure using Geographic Information Systems (GIS). Depending on the type of water system (river system, lake system and tidal system) an interpretation layer of aerial false colour photographs is combined with a water depth layer, a flood duration layer, morphodynamic layer, management layer or a salt gradient layer.

The quality of the ecotope maps is validated on the basis of independent samples of field observations. The total map purity, that is the correctly classified proportion of the map, is estimated for each of the five districts. Besides this, *user's accuracy* and *producer's accuracy* were estimated for each map unit. User's accuracy is the purity of

1 map units: the correctly mapped area of an ecotope relative to the total area of this
2 ecotope *at the map*. It reflects the reliability of the information about an ecotope at the
3 map. Producer's accuracy is the correctly mapped area of an ecotope relative to the total
4 area of this ecotope *in the field*. It indicates the success of the procedures followed in
5 mapping ecotopes.

6 In four districts the validation samples were selected purposively in the past. For the
7 fifth district a probability sample was designed. Sampling points were selected such that
8 the spatial pattern resembles that of the purposive samples.

9 The aim of the study is to compare two sampling approaches for validation of ecotope
10 maps: a model-based and a design-based approach. In the model-based approach sam-
11 pling points are selected by purposive sampling, and a model for the spatial variation of
12 classification errors is used in estimating the map quality measures. In a design-based
13 approach sampling points are selected by probability sampling, and the selection proba-
14 bilities of the sampling points are used in estimating the map quality measures. We will
15 argue that for validation purposes, a design-based sampling approach is recommendable.

16 **2 Definitions of quality measures**

17 The correctly classified proportion of the map or total map purity can be defined as the
18 following areal fraction of an area A :

$$f = \frac{\int_{\mathbf{s} \in A} y(\mathbf{s}) d\mathbf{s}}{|A|}, \quad (1)$$

19 with $|A|$ the surface area of the area A , and

$$y(\mathbf{s}) = \begin{cases} 1 & \text{if } \hat{c}(\mathbf{s}) = c(\mathbf{s}) \\ 0 & \text{else} \end{cases} \quad (2)$$

1 in which $\hat{c}(\mathbf{s})$ is the predicted or mapped ecotope at location \mathbf{s} in area A , and $c(\mathbf{s})$
 2 is the true ecotope at location \mathbf{s} . Map purity is a measure of user's accuracy, because
 3 it informs about the reliability of the map. At the level of individual ecotopes u , user's
 4 accuracy is defined as

$$f_{\text{user},u} = \frac{\int_{\mathbf{s} \in A} y_u(\mathbf{s}) d\mathbf{s}}{\int_{\mathbf{s} \in A} x_u(\mathbf{s}) d\mathbf{s}}, \quad (3)$$

5 with

$$y_u(\mathbf{s}) = \begin{cases} 1 & \text{if } \hat{c}(\mathbf{s}) = c(\mathbf{s}) = u \\ 0 & \text{else} \end{cases} \quad (4)$$

6 and

$$x_u(\mathbf{s}) = \begin{cases} 1 & \text{if } \hat{c}(\mathbf{s}) = u \\ 0 & \text{else} \end{cases} \quad (5)$$

7 The denominator in Eq. (3) is the surface area of map unit (ecotope) u . This area is
 8 known without error, as it can be determined from the map.

9 The producer's accuracy is the extent to which ecotopes which are present in the field
 10 are reflected by the map. It indicates the successfulness of mapping procedures. The
 11 producer's accuracy can be defined as:

$$f_{\text{producer},u} = \frac{\int_{\mathbf{s} \in A} y_u(\mathbf{s}) d\mathbf{s}}{\int_{\mathbf{s} \in A} z_u(\mathbf{s}) d\mathbf{s}}, \quad (6)$$

12 with

$$z_u(\mathbf{s}) = \begin{cases} 1 & \text{if } C(\mathbf{s}) = u \\ 0 & \text{else} \end{cases} \quad (7)$$

13 The denominator in Eq. (6) is the surface area of ecotope u *in the field*. This area is not
 14 known, and must be estimated from the sample.

3 Study areas and validation methods

3.1 Purposively sampled districts

3.1.1 Sampling pattern

Districts 1 to 4 (Figure 2a to d) were sampled purposively. In each of these districts, four to five compact ‘validation areas’ were selected purposively, such that they have a fair spreading over the district, and that they contain all units of the ecotope map. In each of these validation areas a large number of field observations were made at purposively selected locations. Table 1 summarizes the distribution of the sample units over the districts, the validation areas and the ecotopes.

3.1.2 Estimation of map purity

Map purities for the four purposively sampled districts were estimated by model-based inference as described by Lohr (1999). Model-based means that we applied a statistical model of spatial variation of classification errors.

We postulated the following simple *random-effects* model:

$$y_{ij} = \bar{y}_i + \epsilon_{ij} , \tag{8}$$

where

y_{ij} is the indicator at validation point j in validation area i , being 1 if the location has been classified correctly and 0 if not;

\bar{y}_i is the areal fraction being correctly classified in validation area i ;

ϵ_{ij} is the deviation from this areal fraction at location j in validation area i .

We assumed that the stochastic quantity \bar{y}_i has mean μ and variance σ_b^2 , and the stochastic

1 quantity ϵ_{ij} has zero mean and variance σ_w^2 . Further, we assumed that the covariance of
 2 ϵ_{ij} and ϵ_{ik} , $j \neq k$, equals 0.

3 We estimated map purity with the so called ratio estimator, i.e. by the ratio of the
 4 estimated area correctly classified and the estimated total area. Of course, the total area
 5 is known but by dividing by the *estimated* total area, the estimate generally becomes
 6 more accurate. In formula, the ratio estimator equals:

$$\hat{f} = \frac{\frac{N}{n} \sum_{i=1}^n A_i \hat{y}_i}{\frac{N}{n} \sum_{i=1}^n A_i} = \frac{\sum_{i=1}^n A_i \hat{y}_i}{\sum_{i=1}^n A_i}, \quad (9)$$

7 with N the total number of validation areas in the study area, n the number of selected
 8 validation areas, A_i the areal size of the i th validation area, and \hat{y}_i the sample average
 9 of the indicator as defined in Eq. (2) for the i th validation area. The ratio estimator is
 10 model-unbiased under model (8), whatever the areal sizes of validation areas are (Lohr,
 11 1999, p. 165). We estimated the model variance of the correctly classified area following
 12 Lohr (1999, p. 165, Eq. (5.39)).

13 3.1.3 Estimation of user's and producer's accuracy

14 The ratio estimator for the user's accuracy of an individual ecotope u can be obtained by

$$\hat{f}_{\text{user},u} = \frac{\sum_{i=1}^n A_i \hat{y}_{u,i}}{\sum_{i=1}^n A_i \hat{x}_{u,i}}, \quad (10)$$

15 with $\hat{y}_{u,i}$ the sample average of the indicator as defined in Eq. (4) for ecotope u in the
 16 i th validation area, and $\hat{x}_{u,i}$ the sample average of the indicator as defined in Eq. (5) for
 17 ecotope u in the i th validation area.

18 The producer's accuracy of an individual ecotope u is estimated as follows:

$$\hat{f}_{\text{producer},u} = \frac{\sum_{i=1}^n A_i \hat{y}_{u,i}}{\sum_{i=1}^n A_i \hat{z}_{u,i}}, \quad (11)$$

1 with $\hat{y}_{u,i}$ the sample average of the indicator as defined in Eq. (4) for the for ecotope u in
2 the i th validation area, and $\hat{z}_{u,i}$ the sample average of the indicator as defined in Eq. (7)
3 for the for ecotope u in the i th validation area.

4 **3.2 Randomly sampled district ‘Rijn-Maasmonding’**

5 **3.2.1 Sampling constraints**

6 The sampling strategy for the validation of the ecotope map of ‘Rijn-Maasmonding’ had
7 to meet the following budgetary and practical constraints:

- 8 1. The maximum number of observations is 50 per fieldworker per day. Three field-
9 workers are available during ten days. Travel time must be limited in a way that a
10 total sample size of about 1,000 is realistic.
- 11 2. Non-accessible terrain, such as swamps with soft soils, are not part of the target
12 population.
- 13 3. All branches of the rivers must be sampled.
- 14 4. All ecotopes must be validated, excluding water and built-up areas.

15 **3.2.2 A stratified two-stage sample**

16 To meet the first and third constraint, we decided to select sampling points by stratified
17 two-stage sampling. An important advantage of this strategy is that statistical inference
18 is relatively simple as compared to other strategies, such as cluster sampling (de Gruijter
19 et al., 2006). The sampling points were selected such that the spatial pattern resembles
20 that of the purposive samples. This makes practical implementation more easy, because

1 the planning and execution of fieldwork in ‘Rijn-Maasmonding’ is similar to the purpo-
2 sively sampled districts. The procedure of stratified two-stage sampling is as follows:

- 3 1. In the first stage the district ‘Rijn-Maasmonding’ is divided into eight geographical
4 strata, representing the main river branches, and each stratum is divided into val-
5 idation areas (primary sampling units). Figure 3 shows these geographical strata.
6 In each geographical stratum two validation areas are selected by simple random
7 sampling and without replacement.
- 8 2. In the second stage, in each selected validation area a simple random sample of points
9 is taken (the secondary sampling units). Figure 4 shows the selected validation areas
10 and the sampling points.

11 In two-stage sampling the number of sampling points within the primary units must
12 be fixed before the primary sampling units are selected. This condition guarantees that
13 the selection probabilities of the sampling points are known. We made the number of
14 sampling points proportional to the surface areas of the validation areas. Since these
15 surface areas vary, the *total* sample size is not fixed, but varies between samples drawn
16 with the stratified two-stage sampling design. To prevent for large variations of the
17 total sample size in repeated sampling, we delineated the validation areas in such a way
18 that their surface areas within a geographical stratum are approximately constant. The
19 *expected* total sample size is 1,000.

1 3.2.3 Estimation of map purity

2 We estimated map purity with the separate ratio estimator. In this estimator first for
3 each stratum the map purity is estimated by the ratio estimator (see Lohr (1999), p. 148):

$$\hat{f}_h = \frac{\sum_{i=1}^{n_h} A_{hi} \hat{y}_{hi}}{\sum_{i=1}^{n_h} A_{hi}}, \quad (12)$$

4 in which A_{hi} is the area of the i th selected primary unit in stratum h , and \hat{y}_{hi} the estimated
5 areal fraction being correctly classified in the i th primary unit in stratum h . This fraction
6 is estimated by the sample average of the indicators of Eq. (2) at the m_{hi} sampling points
7 in validation area i in geographical stratum h :

$$\hat{y}_{hi} = \frac{1}{m_{hi}} \sum_{j=1}^{m_{hi}} y_{hij}. \quad (13)$$

8 Finally, The ratio estimator of the map purity of the total area is estimated by

$$\hat{f} = \sum_{h=1}^{\ell} w_h \hat{f}_h, \quad (14)$$

9 with

$$w_h = \frac{A_h}{\sum_{h=1}^{\ell} A_h}.$$

10 For the calculation procedure of the sampling variance of the ratio estimators we refer to
11 Lohr (1999, p. 148).

12 3.2.4 Estimation of user's and producer's accuracy

13 The user's accuracy or map purity per ecotope was again estimated by the *separate* ratio
14 estimator.

15 The user's accuracy of map unit u in stratum h was estimated by

$$\hat{f}_{\text{user},u,h} = \frac{\sum_{i=1}^{n_h} A_{hi} \hat{y}_{u,hi}}{\sum_{i=1}^{n_h} A_{hi} \hat{x}_{u,hi}}, \quad (15)$$

1 with $\hat{y}_{u,hi}$ and $\hat{x}_{u,hi}$ the sample averages of the indicators of Eqs. (4) and (5), respectively,
 2 for ecotope u in the i th validation area in the h th stratum.

3 For the district ‘Rijn-Maasmonding’ the user’s accuracy of ecotope u is estimated by:

$$\hat{f}_{\text{user},u} = \sum_{h=1}^{\ell} w_h \hat{f}_{\text{user},u,h} . \quad (16)$$

4 The producer’s accuracy of an ecotope u in stratum h was estimated by

$$\hat{f}_{\text{producer},u,h} = \frac{\sum_{i=1}^{n_h} A_{hi} \hat{y}_{u,hi}}{\sum_{i=1}^{n_h} A_{hi} \hat{z}_{u,hi}} , \quad (17)$$

5 with $\hat{z}_{u,hi}$ the sample average of the indicator of Eq. (7) for ecotope u in the i th primary
 6 unit in stratum h . The producer’s accuracy of ecotope u for the total area of ‘Rijn-
 7 Maasmonding’ is estimated with

$$\hat{f}_{\text{producer},u} = \sum_{h=1}^{\ell} w_h \hat{f}_{\text{producer},h,u} . \quad (18)$$

8 4 Results

9 The first eight columns in Table 2 show the validation results for the four purposively
 10 sampled areas, the last two columns contain the validation results for the randomly sam-
 11 pled district “Rijn-Maasmonding”. Note that areal fractions have been converted to
 12 percentages. Relatively low accuracies might have several sources, such as:

- 13 1. During the fieldwork for validation observation errors have been made, for instance
 14 due the impossibility to observe in the field all values of the several indicators (for
 15 example flood duration) which are used to generate an ecotope map;
- 16 2. During the time between the shots of aerial photographs and the fieldwork for
 17 validation the vegetation might have changed;

- 1 3. The information on which the maps are based might be imperfect;
- 2 4. Errors might have been made in interpreting this information;
- 3 5. Cartographic errors might have been made in delineating ecotopes.

4 The total map purities vary from 56 to 76 %. The map purity of the randomly sampled
5 district “Rijn-Maasmonding” is estimated more accurately than those of the four pur-
6 posively sampled districts: a standard error of 2 % vs. standard errors varying from 5
7 to 9 %. Note that the standard errors of map purities for the four purposively sampled
8 districts were possibly underestimated, because in the random effects model we assumed
9 that the errors were spatially uncorrelated. The relatively accurate estimate of map purity
10 for “Rijn-Maasmonding” can be explained from (i) a larger number of sampling points
11 (902 versus 266 to 406), and (ii) a better spatial distribution of the validation areas (16
12 versus 4 to 5).

13 **5 Discussion and conclusions**

14 This study compared two methods of validating ecotope maps: purposive sampling com-
15 bined with a model-based estimation method, and probability sampling combined with a
16 design-based estimation method. In both methods the sampling points were clustered in a
17 limited number of compact validation areas, in order to reduce travel costs. In estimating
18 map purities and user’s and producer’s accuracies for IJsselmeer, Volkerak-Zoommeer,
19 Rijntakken and Maas a random effects model was applied, which implied assumptions on
20 the distribution of the classification errors. We demonstrated that stratified two-stage
21 sampling is an alternative to purposive sampling, answering to the same practical and

1 budgetary constraints. Stratified two-stage sampling combined with a design-based es-
2 timation method results in model-free estimates of map purity, user's and producer's
3 accuracies. This is an important advantage in validation, because the results do not de-
4 pend on the quality of model assumptions (Brus and de Gruijter, 1997). This means that
5 the validity of the estimated map purities, user's and producer's accuracies is beyond
6 discussion if a design-based approach is followed.

7 As a consequence of the model assumptions made in the validation of IJsselmeer,
8 Volkerak-Zoommeer, Rijnakken and Maas the standard errors of the estimated map
9 purities were possibly underestimated. The design-based approach followed for Rijn-
10 Maasmonding has the advantage that no model is used in calculating standard errors of
11 map purities.

12 **Acknowledgments**

13 This study was supported by the project EBONE of the European Union. The work on
14 GIS by Mrs. Nanny Heidema (Alterra-Wageningen University and Research Centre) was
15 indispensable to complete this study. We are grateful to Drs. Gertrud Houkes (Ministry
16 of Public Works, Transport and Water Management) for providing us with data, and for
17 her useful comments on the manuscript.

18 **References**

19 Brus, D. J. and de Gruijter, J. J. (1997). Random sampling or geostatistical modelling?
20 Choosing between design-based and model-based sampling strategies for soil (with Dis-
21 cussion). *Geoderma*, 80:1–59.

- 1 de Gruijter, J. J., Brus, D. J., Bierkens, M. F. P., and Knotters, M. (2006). *Sampling for*
2 *Natural Resource Monitoring*. Springer, Berlin.
- 3 Girel, J., Garguet-Duport, B., and Pautou, G. (1997). Landscape structure and histor-
4 ical processes along diked European valleys: a case study of the Arc/Isère confluence
5 (Savoie, France). *Environmental Management*, 21:891–907.
- 6 Lohr, S. (1999). *Sampling: Design and Analysis*. Duxbury Press, Pacific Grove, USA.
- 7 Stumpel, A. and Kalkhoven, J. (1978). A vegetation map of the Netherlands, based on
8 the relationship between ecotopes and types of potential natural vegetation. *Vegetatio*,
9 37:163–173.
- 10 Wolfert, H. P. (1996). Rijkswateren-Ecotopen-Stelsels. Uitgangspunten en plan van aan-
11 pak. (In Dutch, with Summary in English). Technical Report 96.050, RIZA, Lelystad,
12 Netherlands.

Table 1: Summary of validation samples in the four purposively sampled districts

District	number of validation areas	total number of validation points	number of validation points per validation area
IJsselmeer	4	369	69, 137, 94, 69
Volkerak-			
Zoommeer	5	266	78, 43, 36, 51, 58
Rijntakken	5	406	82, 44, 47, 143, 90
Maas	4	362	76, 128, 106, 52

Table 2: Validation results. U = user's accuracy (%), P = producer's accuracy (%)

Ecotope group	District									
	IJsselmeer		Maas		Rijntakken		Volkerak-Zoommeer		Rijn-Maasmonding	
	U	P	U	P	U	P	U	P	U	P
arable land	30	73	79	82	78	89	-	0	69	99
bare	70	92	47	73	62	78	50	73	76	97
rough herbage	27	45	37	36	58	55	29	12	39	51
forest	64	67	74	87	68	77	60	79	82	61
grassland	89	68	90	80	73	83	75	62	88	51
helofytes	78	68	0	0	69	59	45	77	74	62
osier-thicket	-	-	-	0	0	0	-	-	35	83
shrub	27	44	36	44	48	41	42	66	43	63
solid substrate	82	78	67	68	87	48	100	32	17	18
water	-	-	-	-	-	-	-	0	-	-
Total purity (s.e.)	70(5)		74(7)		69(5)		56(9)		76(2)	

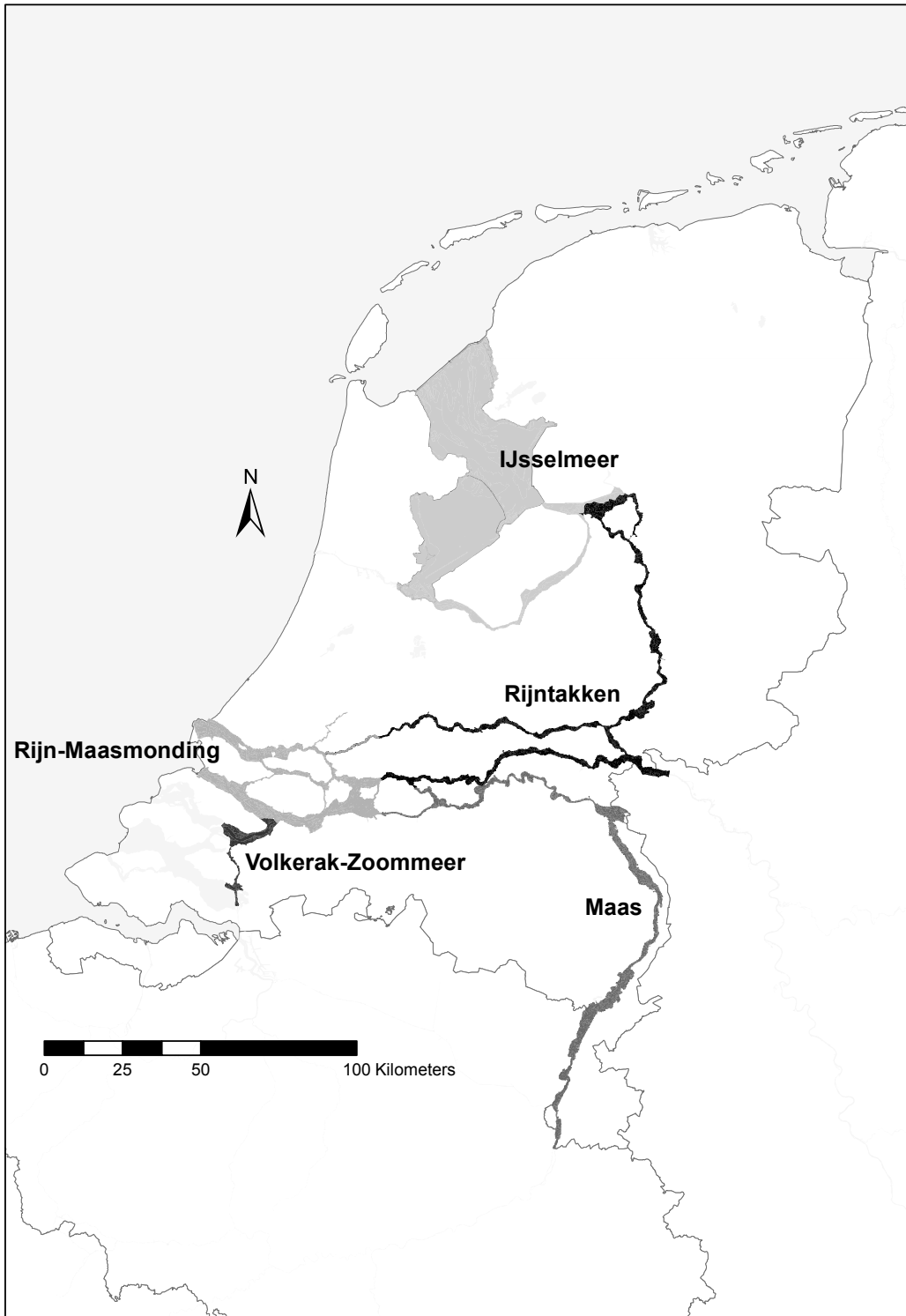


Figure 1: Districts of main watercourses in the Netherlands

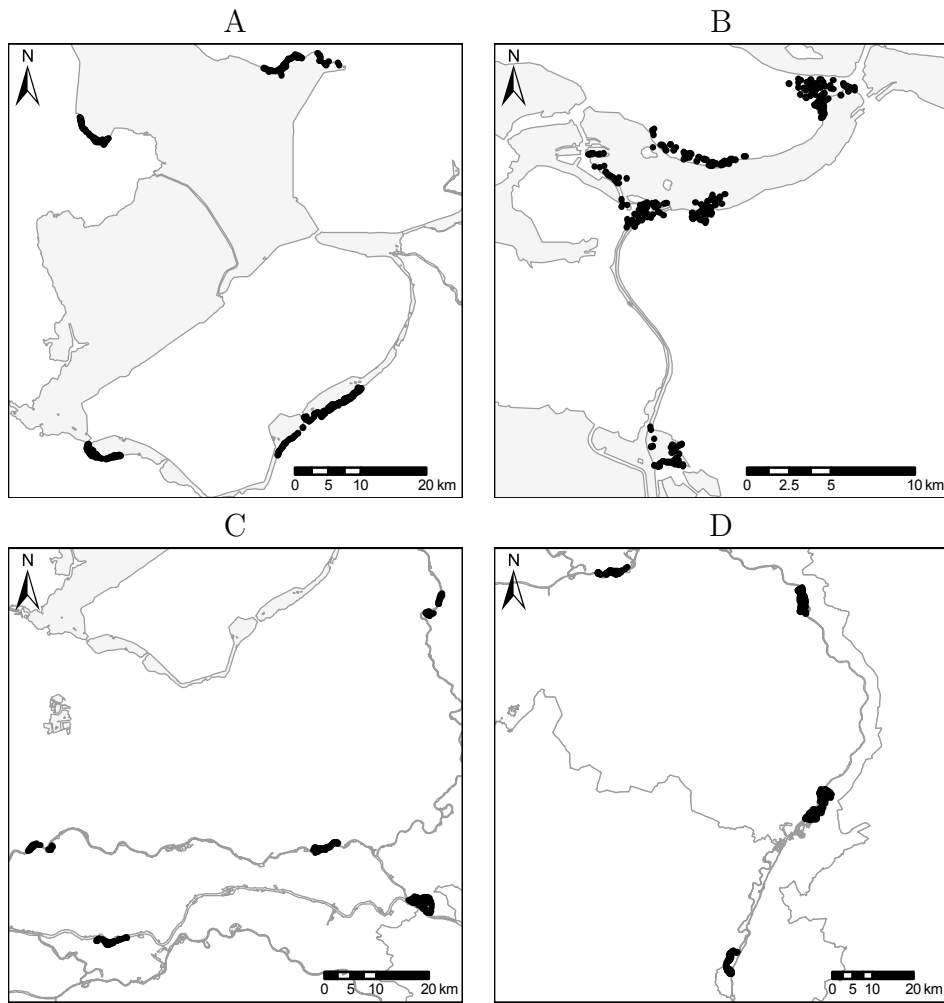


Figure 2: Sampling patterns in the purposively sampled districts. A: IJsselmeer, B: Volkerak-Zoommeer, C: Rijntakken, D: Maas

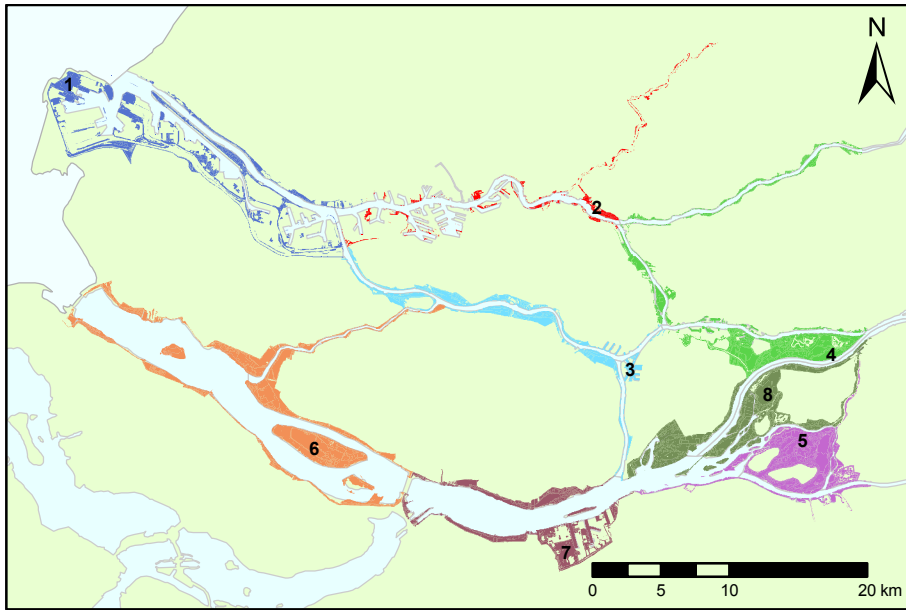


Figure 3: Geographical strata of the district 'Rijn-Maasmonding'

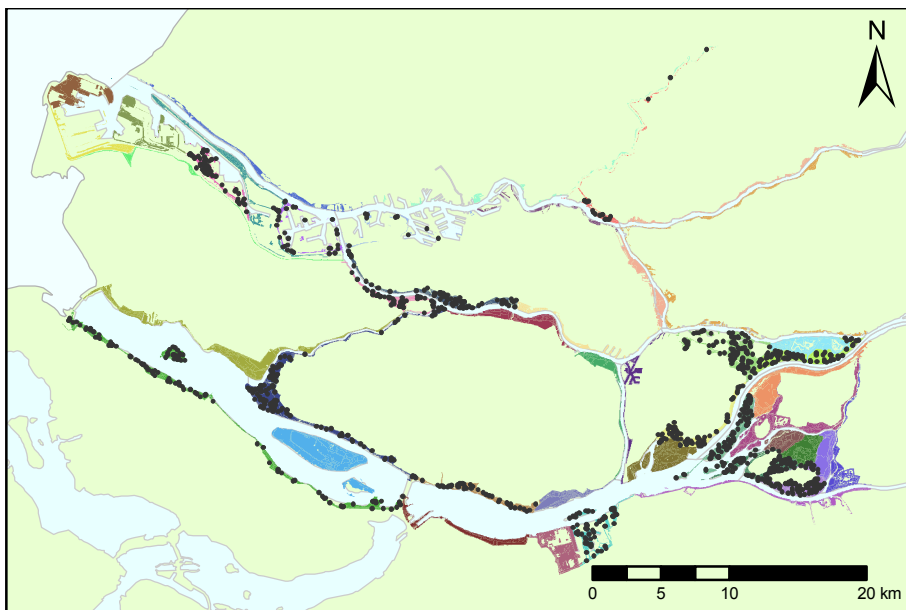


Figure 4: Location of validation areas and sampling points in “Rijn-Maasmond”